University of Massachusetts Amherst

Featuring NICHOLAS G. REICH

How to Forecast a Pandemic: Lessons from COVID-19

AN A REAL PROPERTY AND ADDRESS

Distinguished Faculty Lecture Series 2021

BE REVOLUTIONARYTM



I'm telling you stories. Trust me. from "The Passion" by Jeanette Winterson

This data-driven story is about our journey to learn more about epidemic modeling

- what approaches produce best predictions of outbreaks in general
- how reliable have models been in predicting COVID-19
- how can we use multiple models to improve predictions

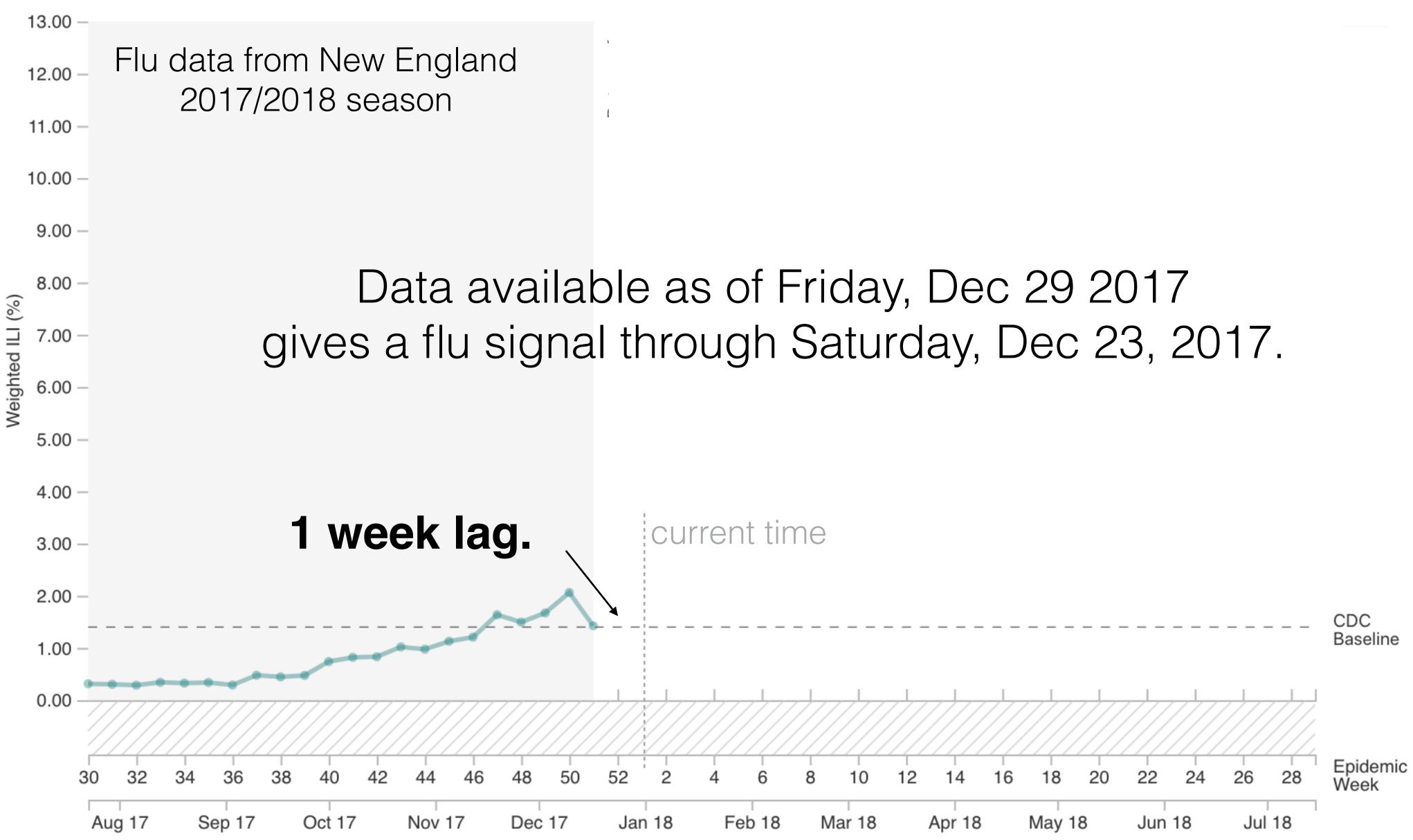
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In God we trust; all others bring data. W. Edwards Deming

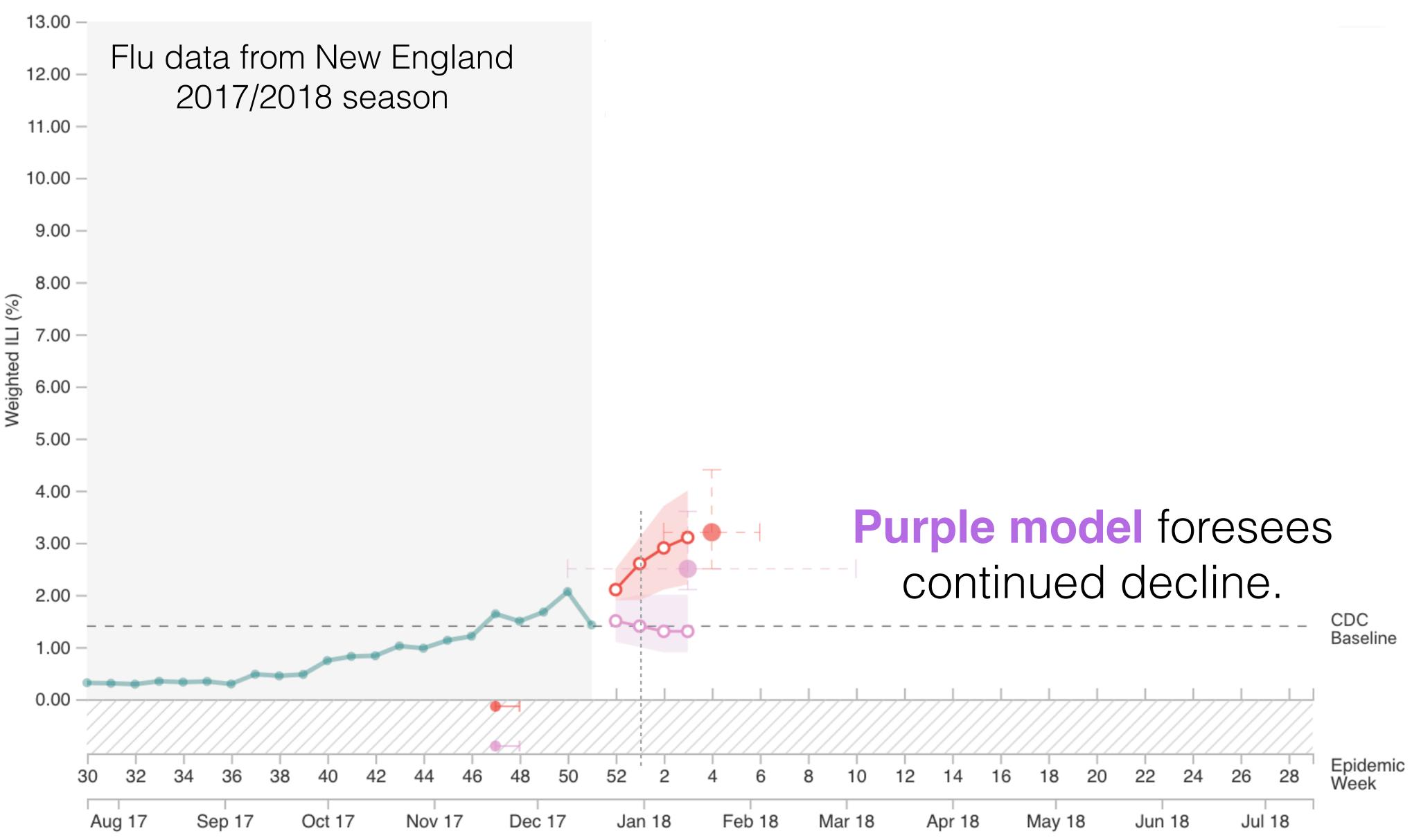
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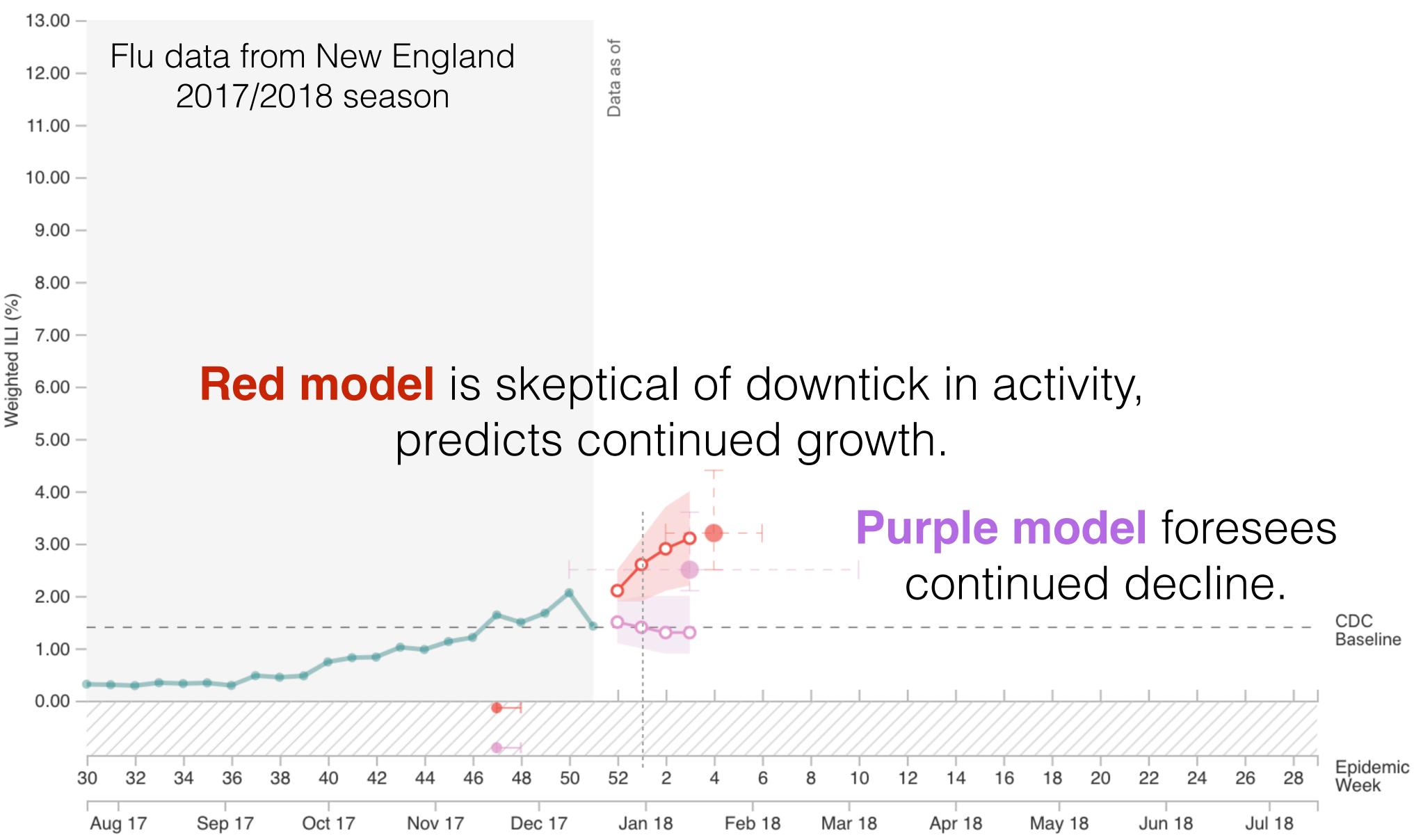
Preface



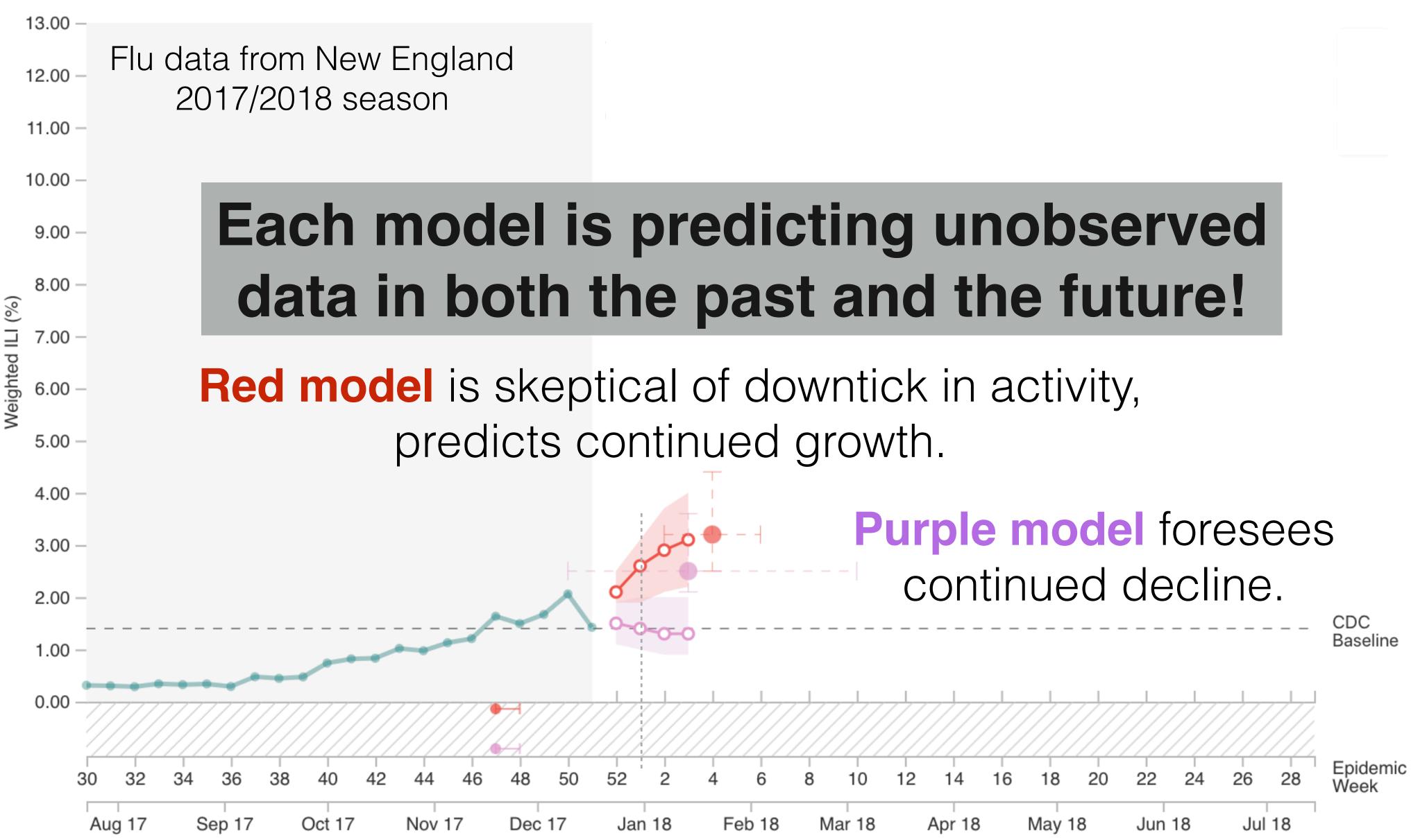




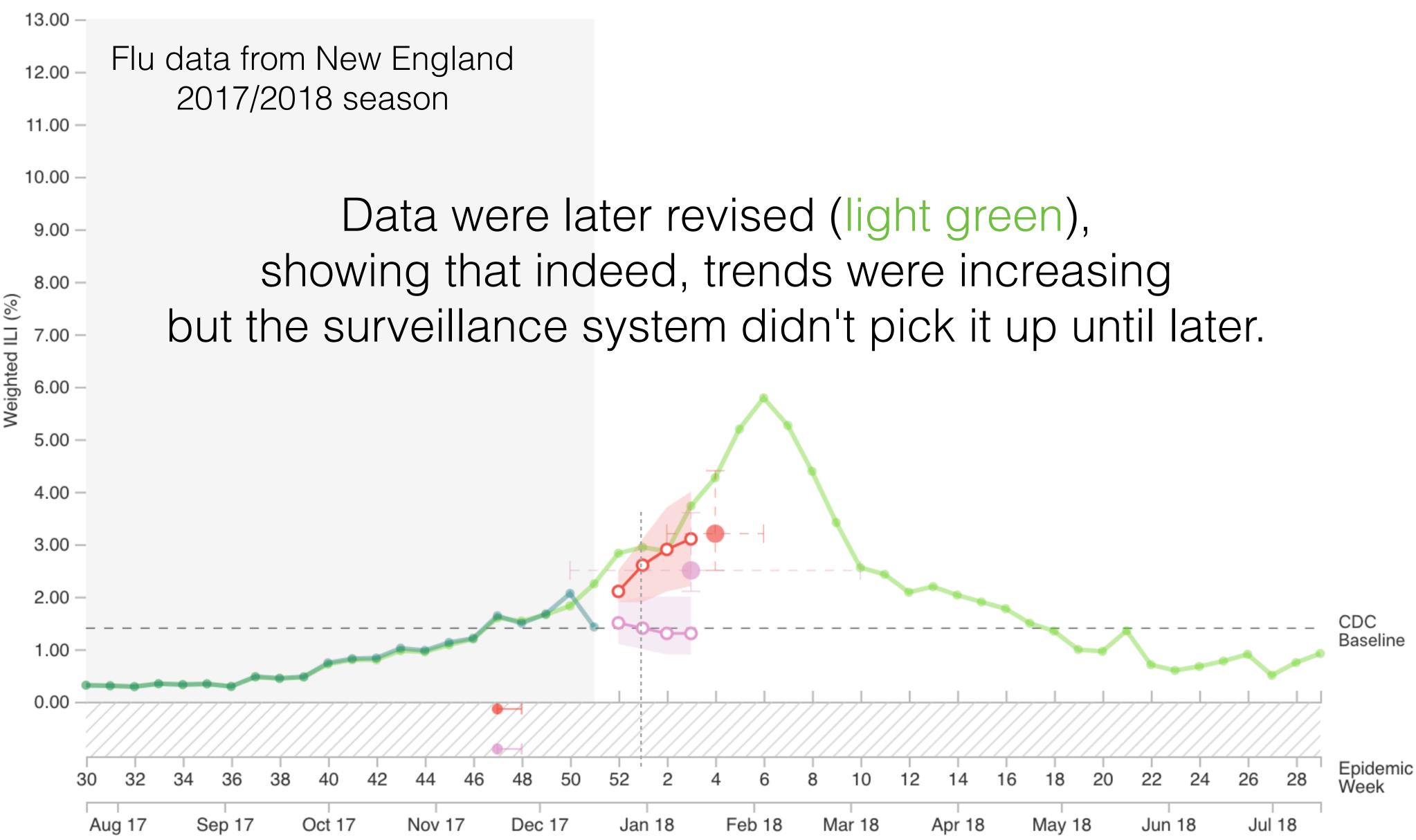




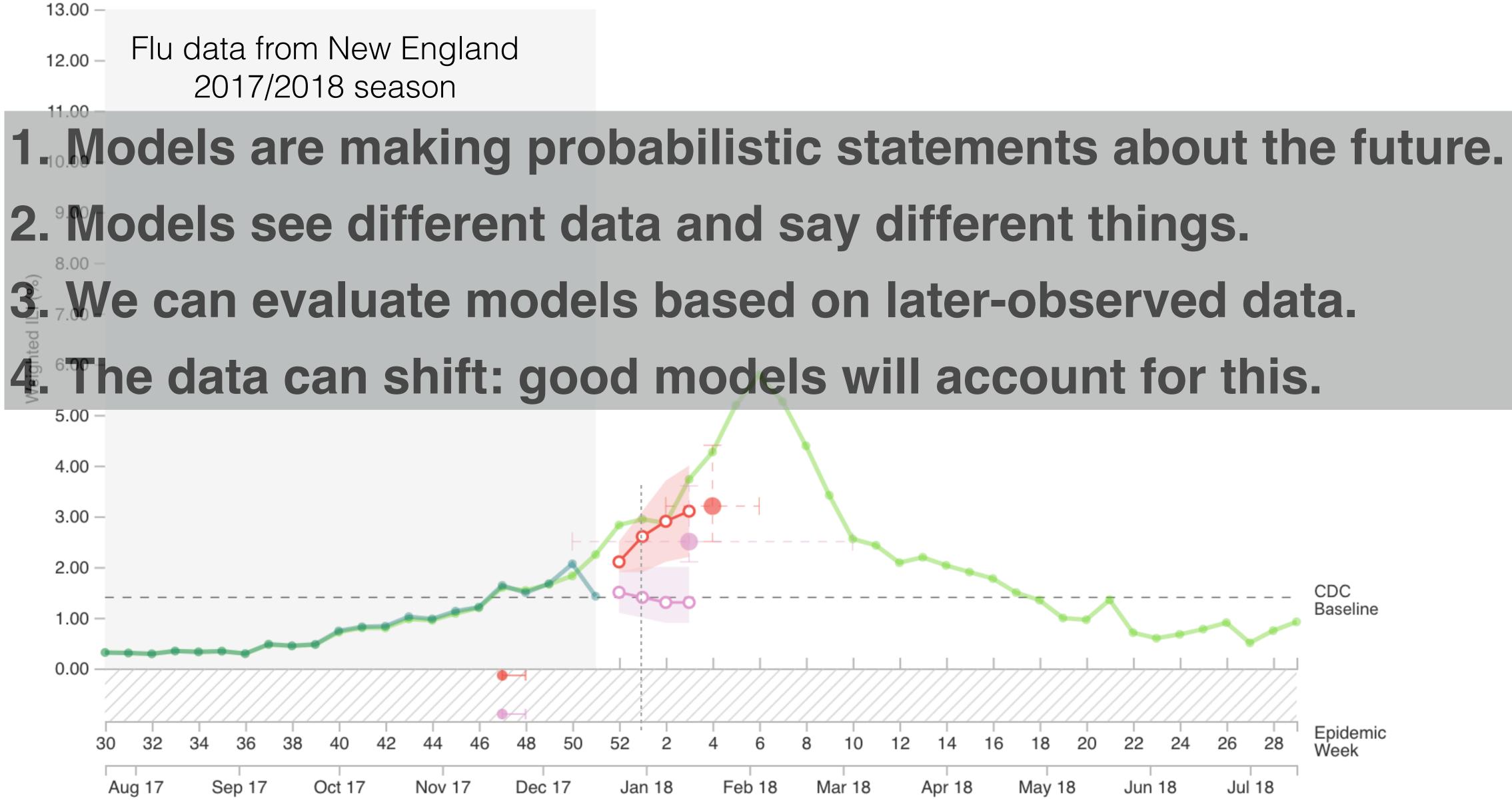
















Chapter 1: An abstraction

Statistical Science 2001, Vol. 16, No. 3, 199-231

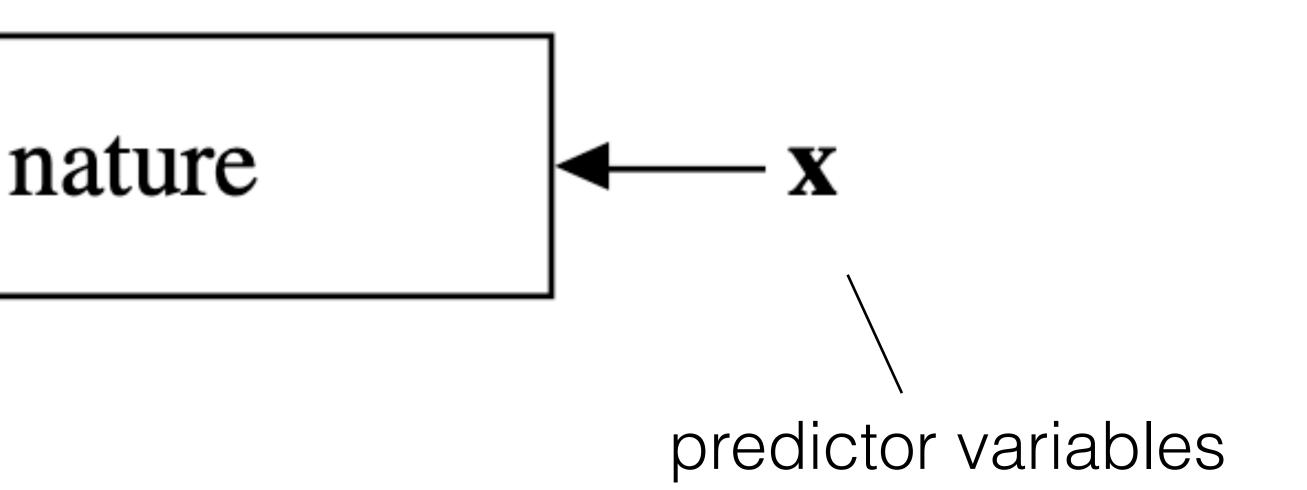
Statistical Modeling: The Two Cultures

Leo Breiman

Data arise thanks to the black box of nature.

outcome variable

e.g. covid cases next week in Hampshire county



covid cases this week, behavior, vaccination, cases in all past weeks, ...



Statistical Science 2001, Vol. 16, No. 3, 199–231

Statistical Modeling: The Two Cultures

Leo Breiman

One goal: infer something about nature from data.



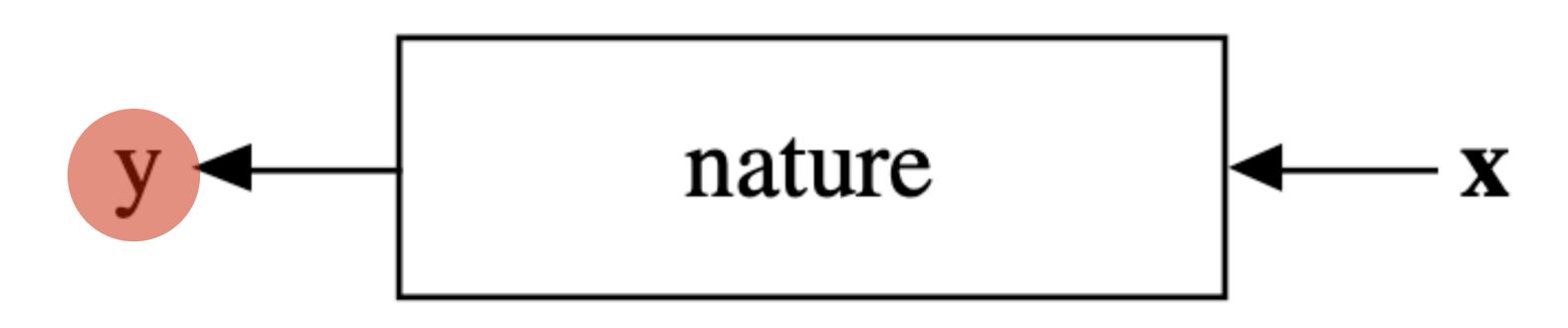
We want to learn something about the "true" state of nature, but we will never be able to observe what the black box relationships are between all the \mathbf{x} and y.

How do population structure, human behavior, biological features of a pathogen, etc... interact to cause an outbreak?

"To extract some information about how nature is associating the response variables to the input variables."

Statistical Modeling: The Two Cultures

Leo Breiman



In prediction, we might be less concerned learning about nature, and more with what the the outcome y will be. If we are careful, we can pick problems and settings where we can (eventually) know the truth about what y will be given some **x**.

How many cases will be observed next week?

"To be able to predict what the responses are going to be to future input variables."

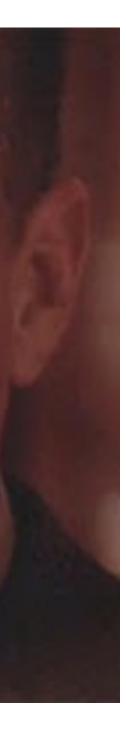




Philosophical differences btw. prediction and inference

- With predictive modeling, in many cases, we will eventually see the "truth" and we will have a direct measure of the quality of our model.
- With inferential modeling, the "truth" remains forever elusive.
- This talk focuses on scientific challenges where we eventually get to see the "truth" (or a reasonable approximation of it).

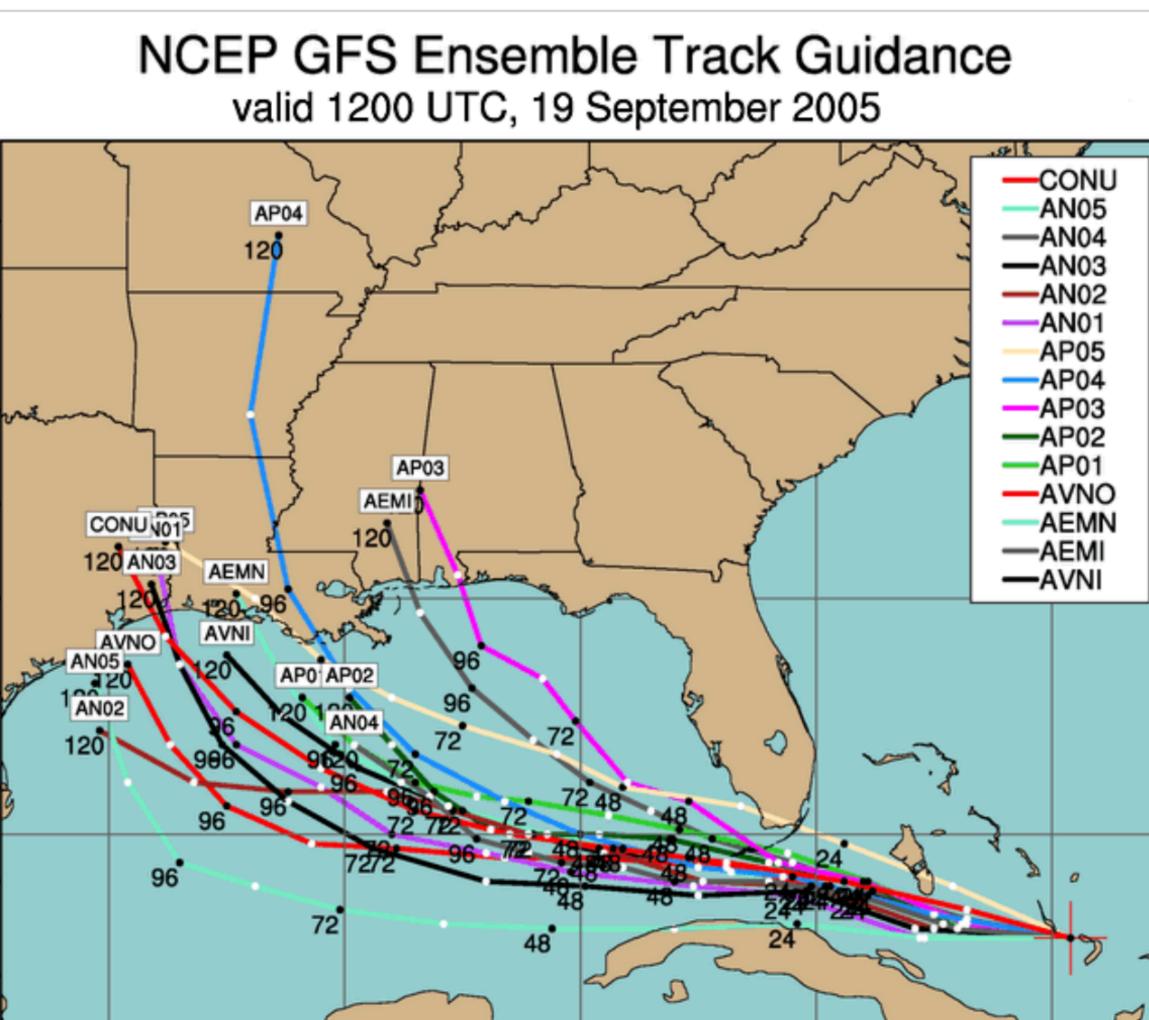
YOU CAN'T HANDLE TUBIE TRUTH!



The best approximations of truth involve multiple perspectives

 "Ensemble" forecasts, or combinations of predictions from different models, are a goldstandard in many fields focused on predictive modeling: climate, weather, economics, sports, etc...

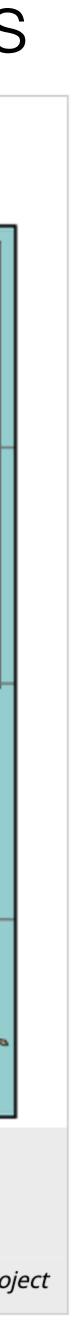
• There are formal mathematical reasons for why this approach works, but the concepts behind the "wisdom of the crowd" approach are intuitive.



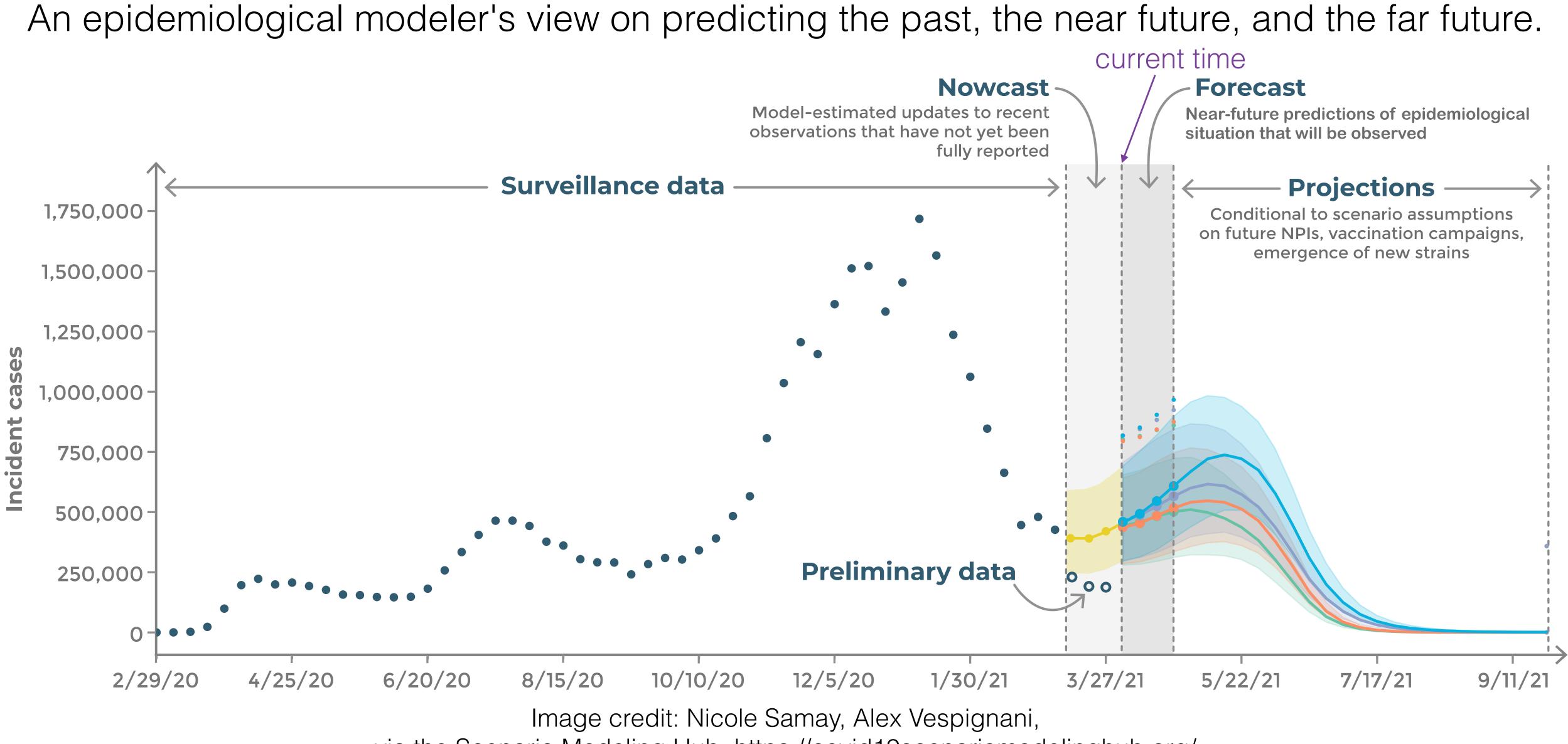
The GFS Ensemble track forecast for Hurricane Rita, initialized at 12Z on September 19, 2005, showed good agreement among the ensemble members in the short term, but less agreement after 24 hours.

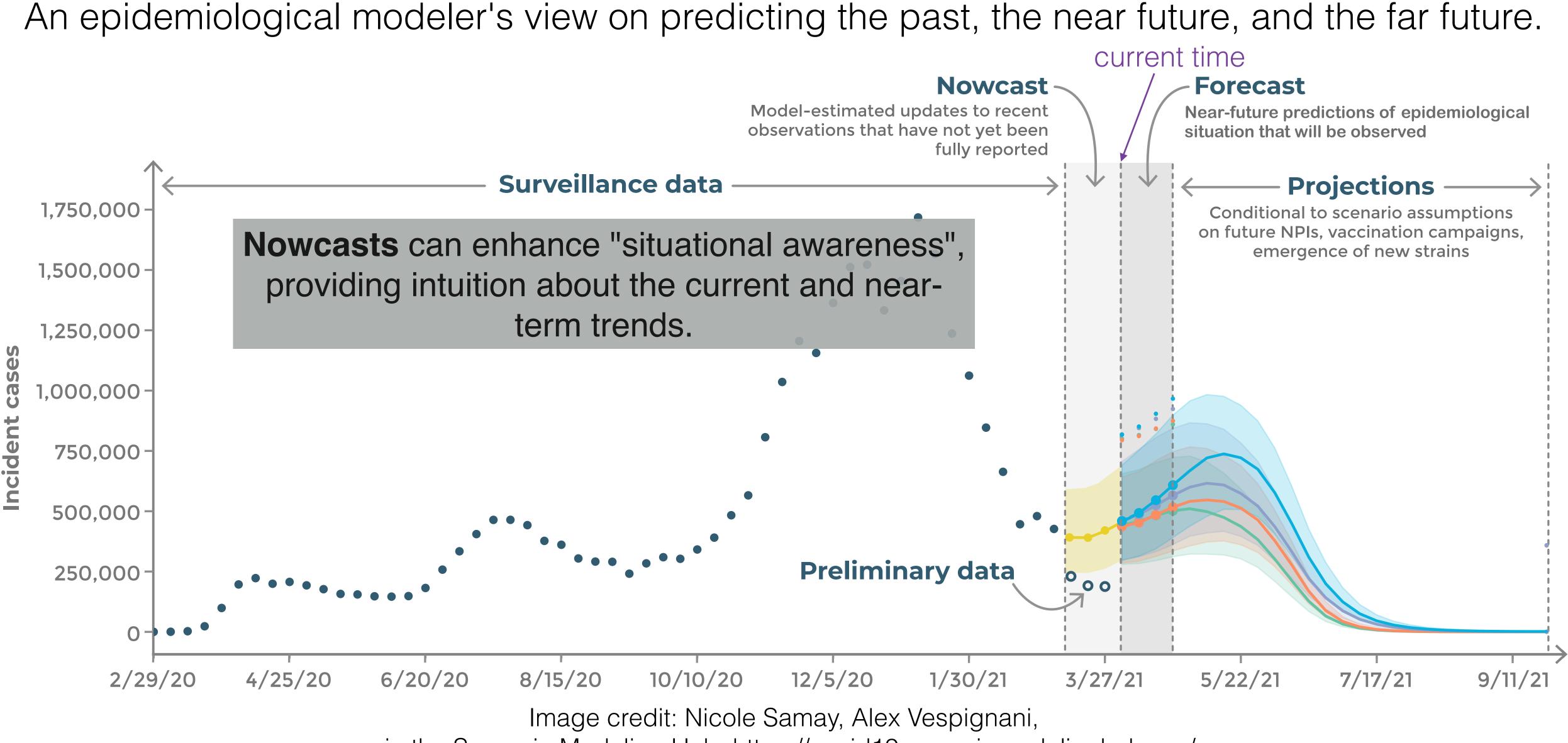
Credit: NCAR Tropical Cyclone Guidance Project

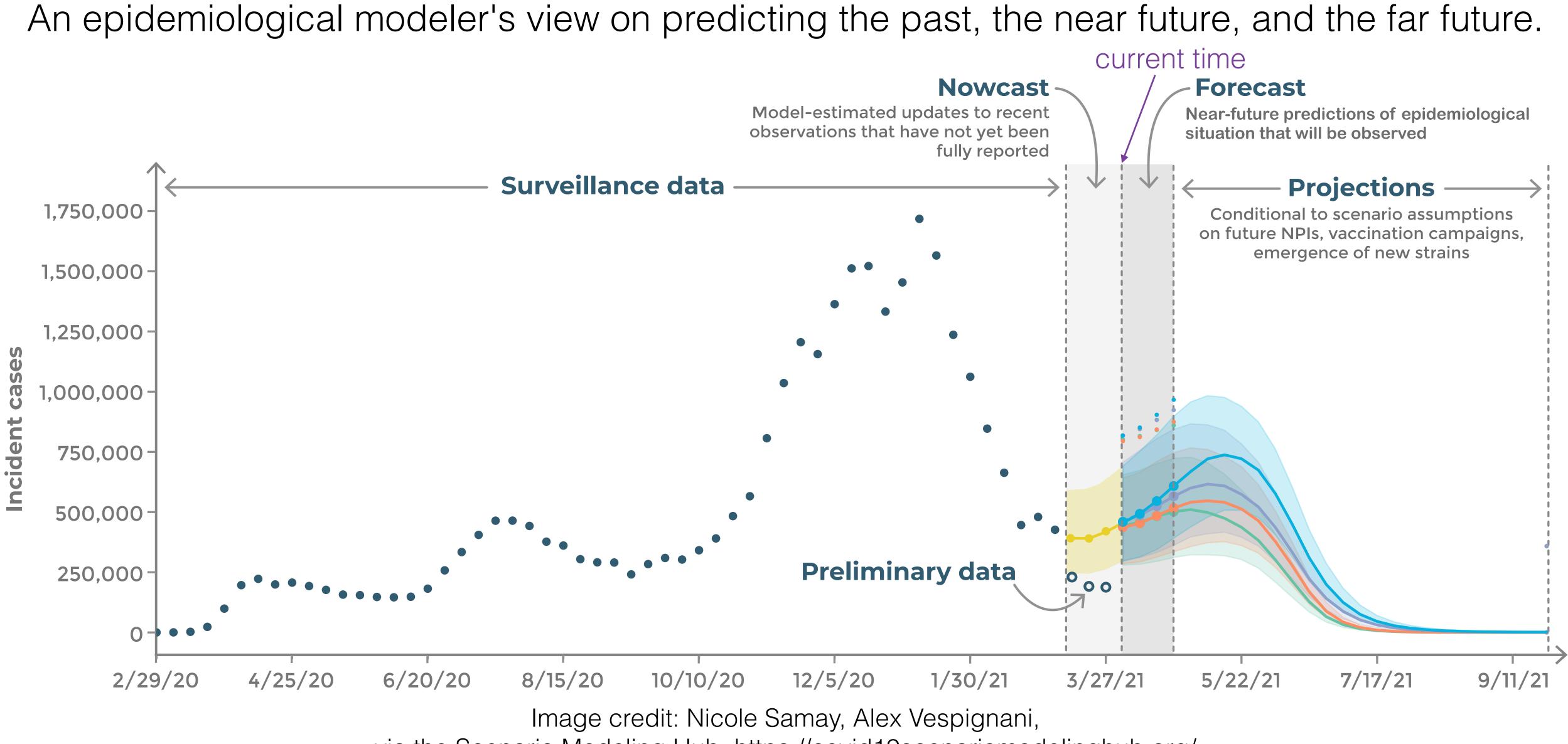
https://learningweather.psu.edu/node/60

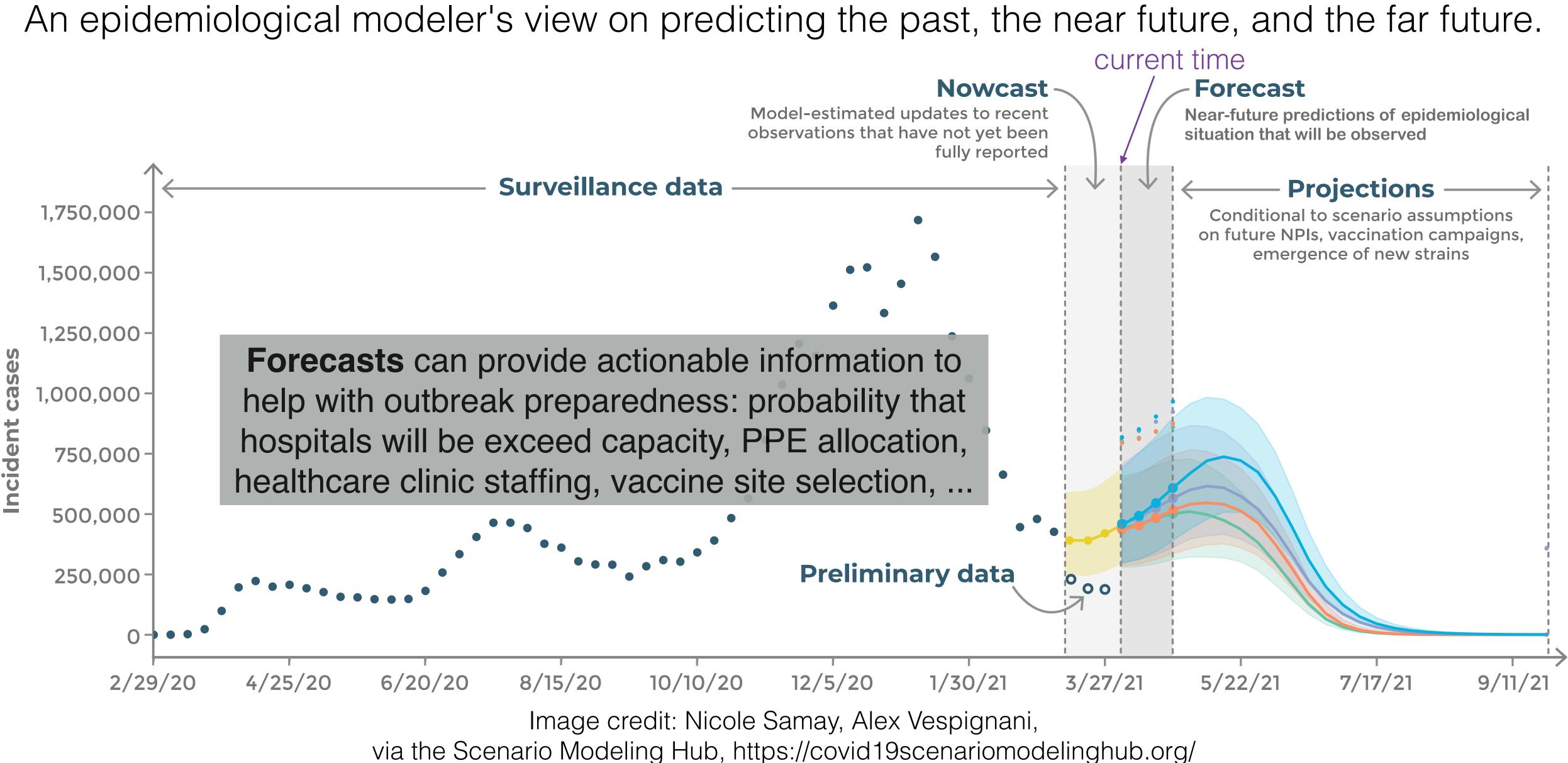


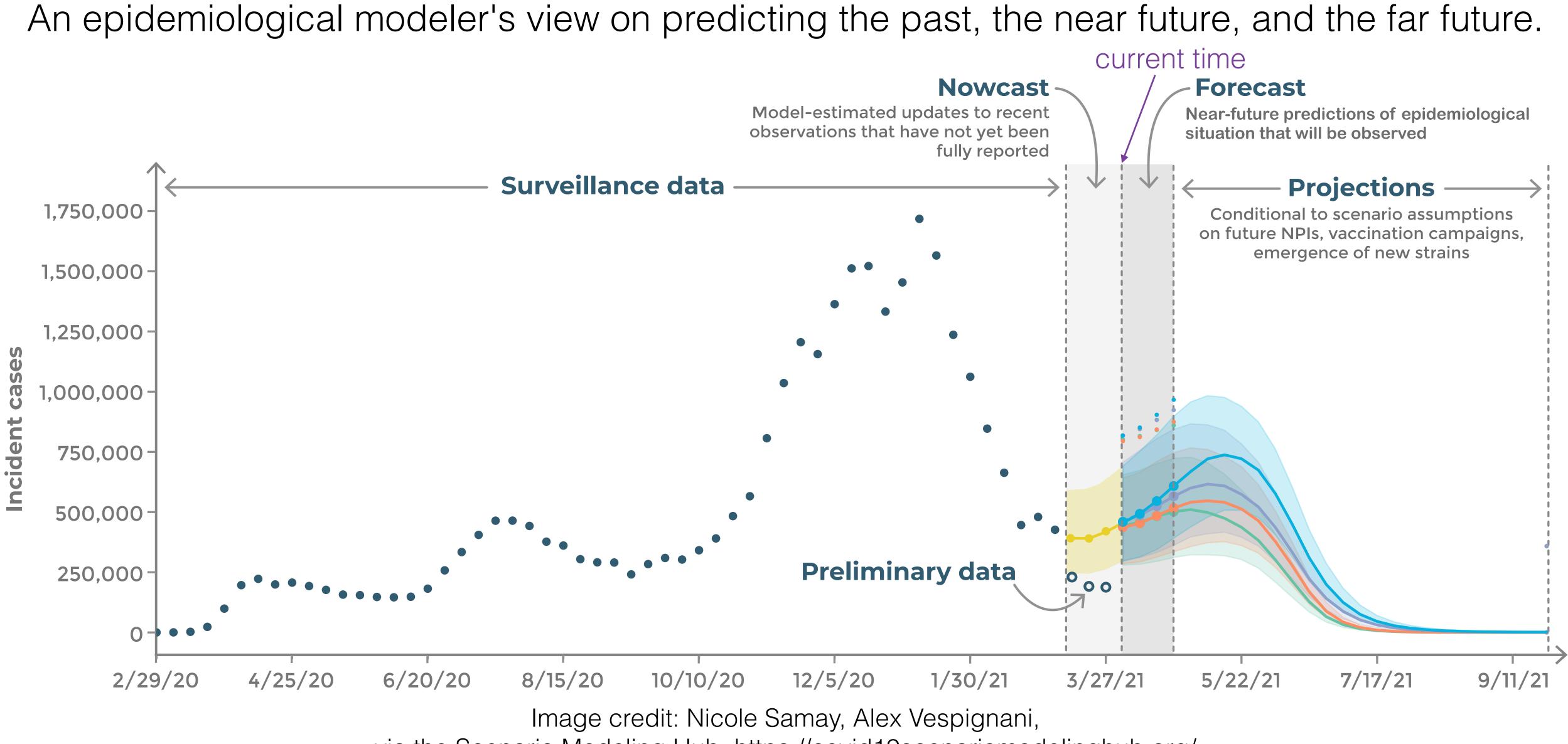
Chapter 2: background on epidemic forecasting

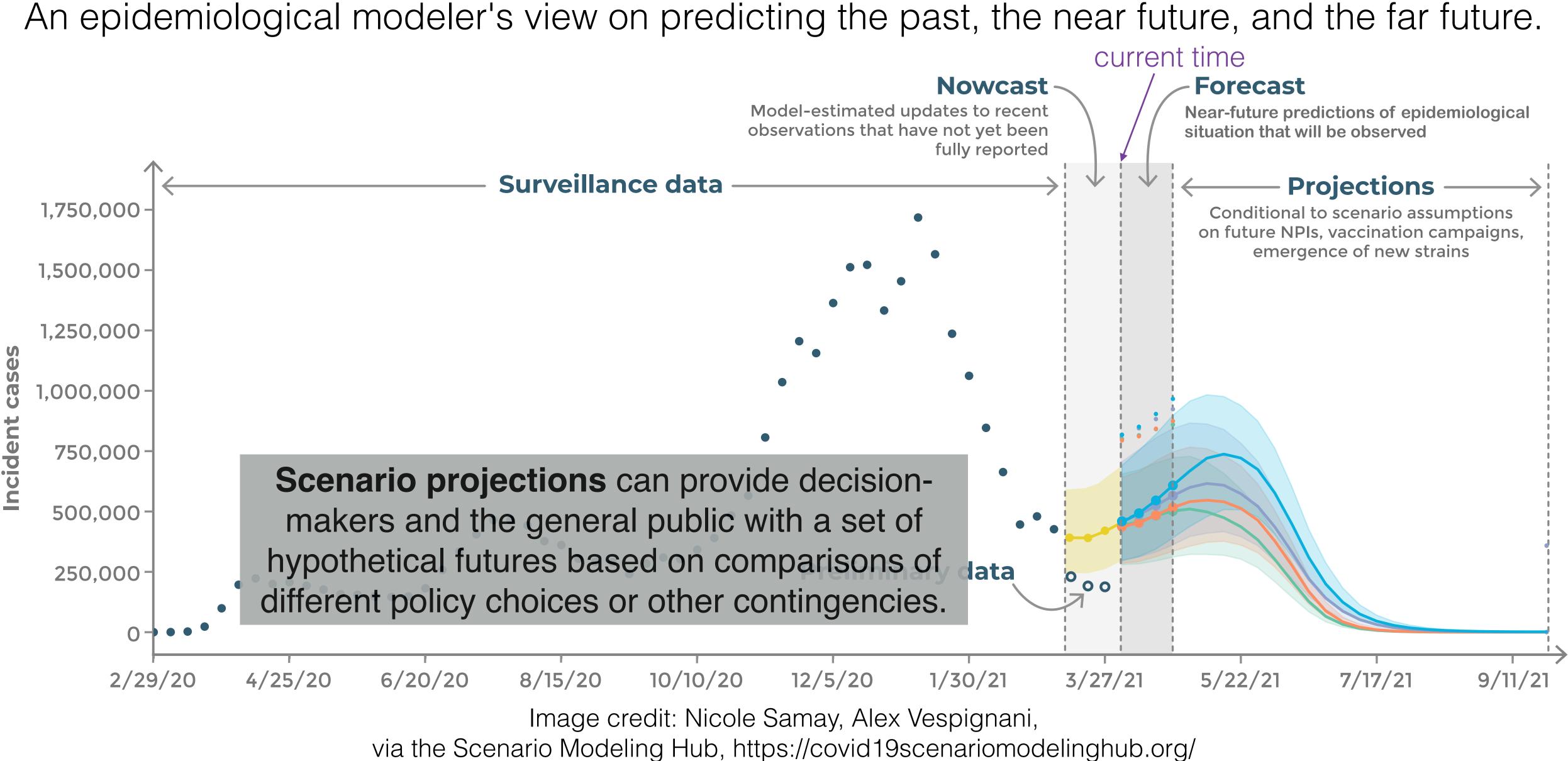


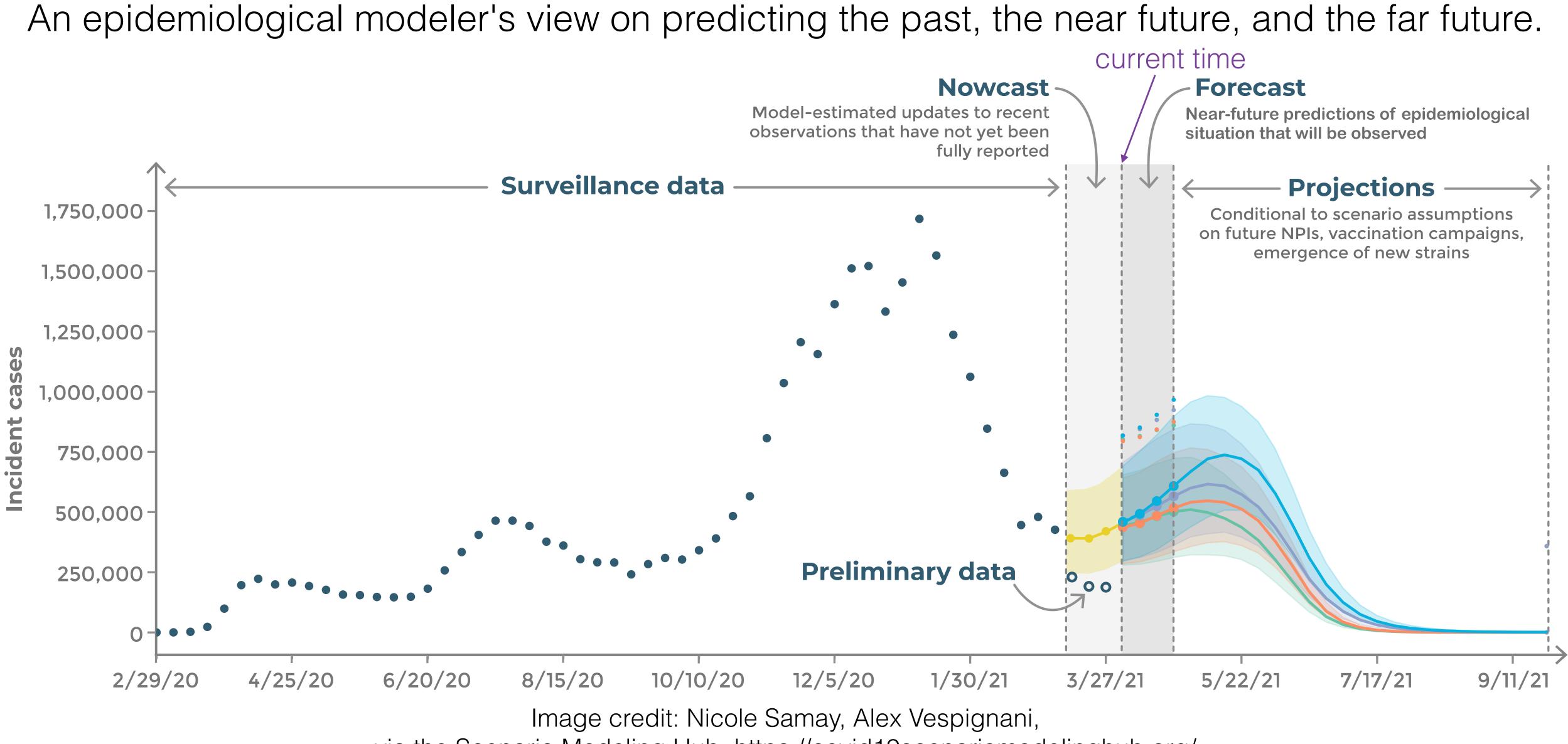


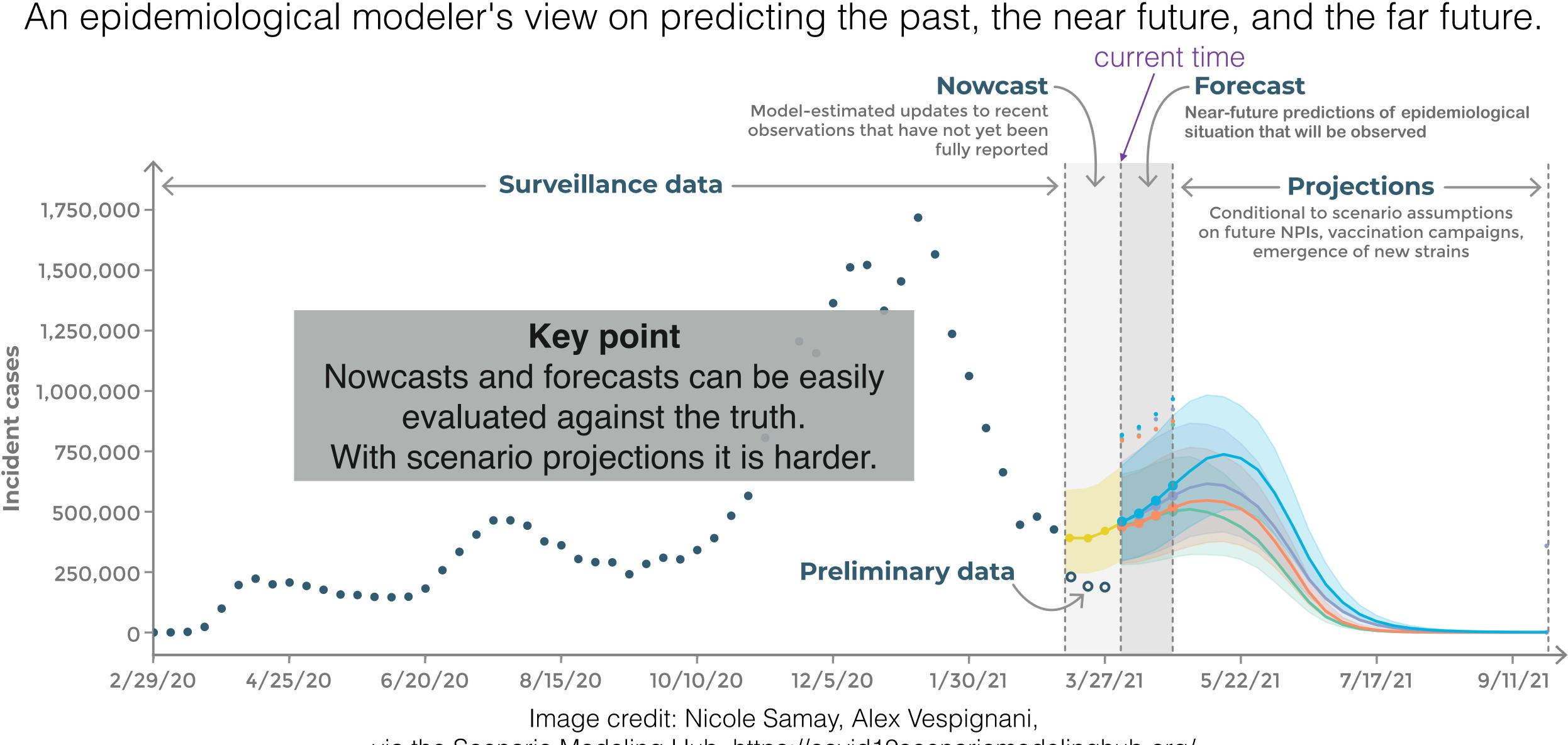












Challenge: data sparsity

(infectious disease dynamics cannot be observed like the weather)

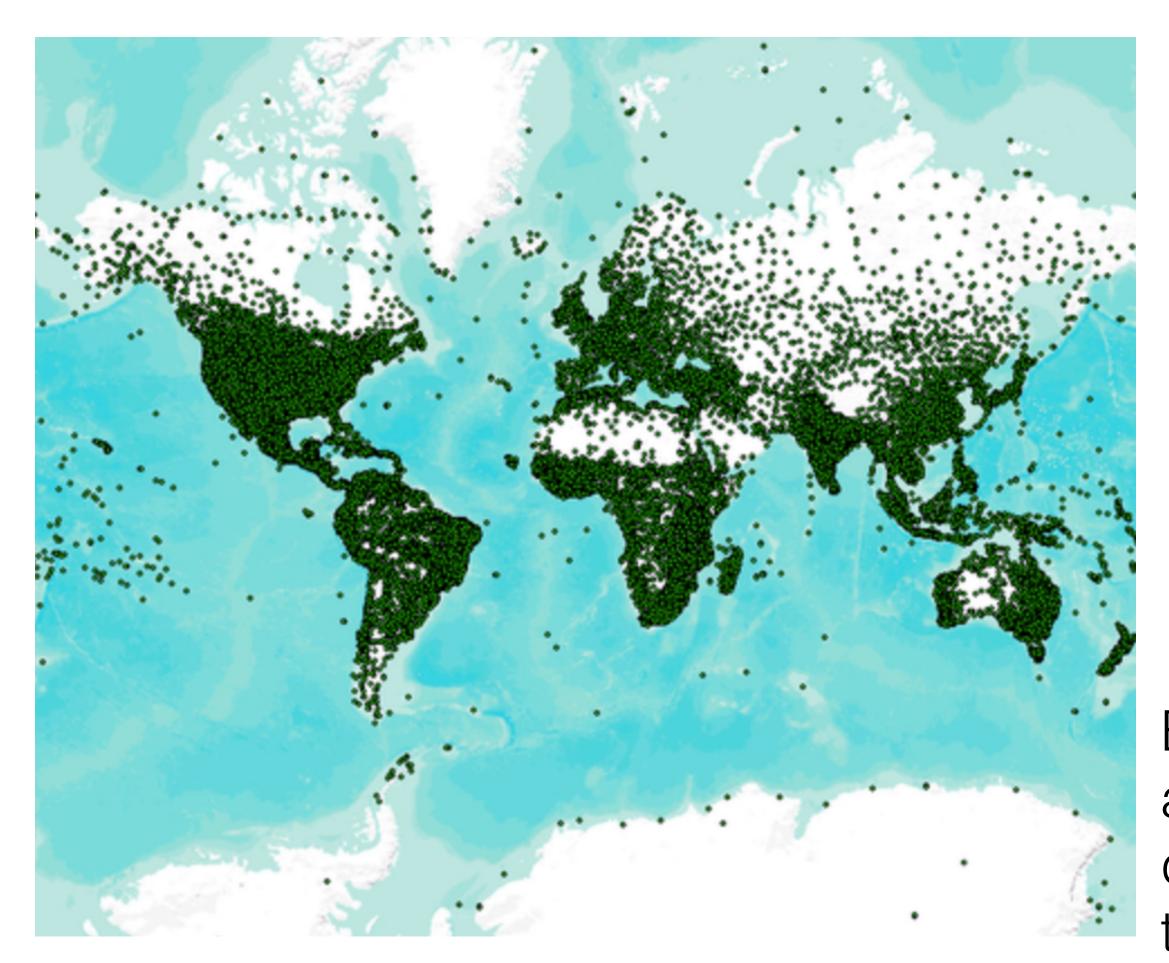


image credit: https://databasin.org/datasets/15a31dec689b4c958ee491ff30fcce75



Each dot represents a weather station whose data was used to create the WorldClim dataset.

image credit: <u>https://goo.gl/images/CSSQRv</u>



Challenge: epidemic forecast feedback loop

- Weather forecasts don't impact the weather.
- An outbreak forecast or projection could impact an outbreak.



2014: US military troops heading to Liberia to assist with Ebola outbreak. image: <u>defense.gov</u>

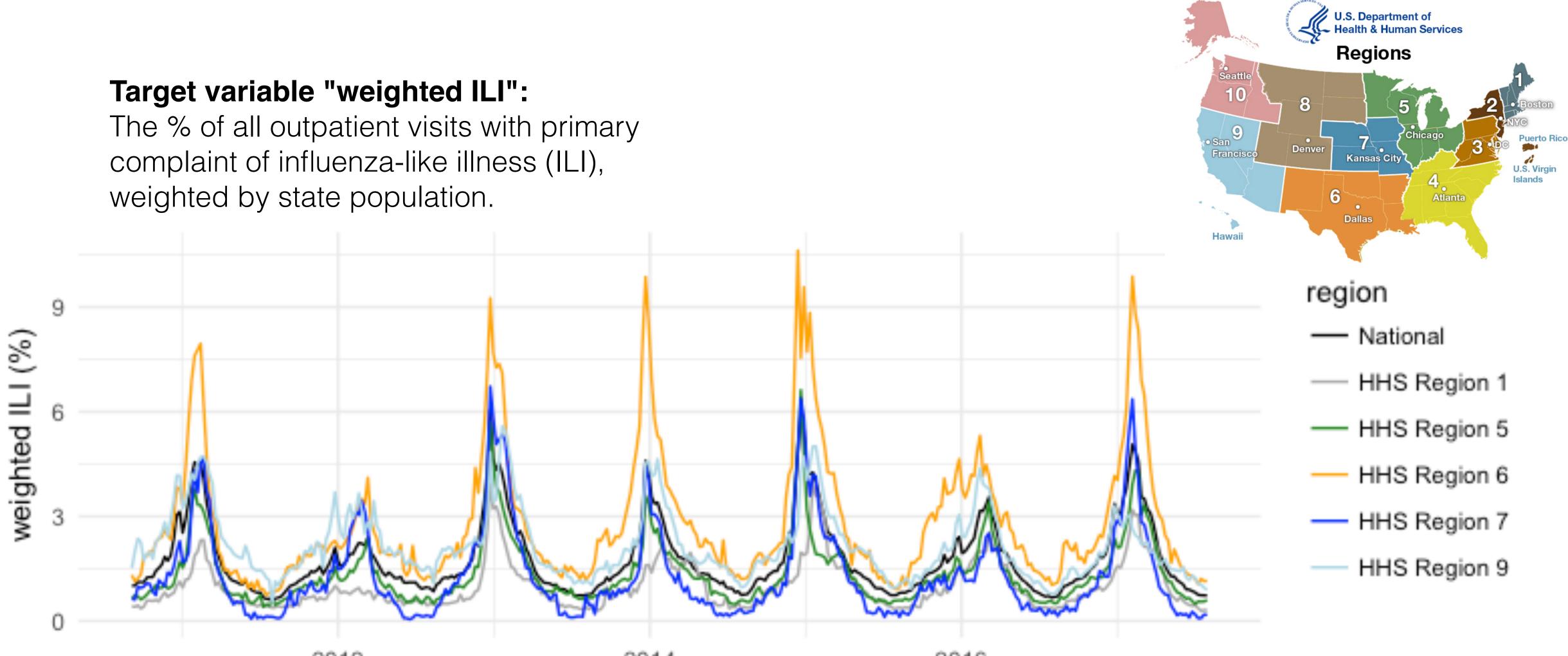
2018: vector-control activities to prevent dengue in Thailand courtesy of Sopon lamsirithaworn, Thailand Department of Disease Control



Typical epidemic forecasting setup

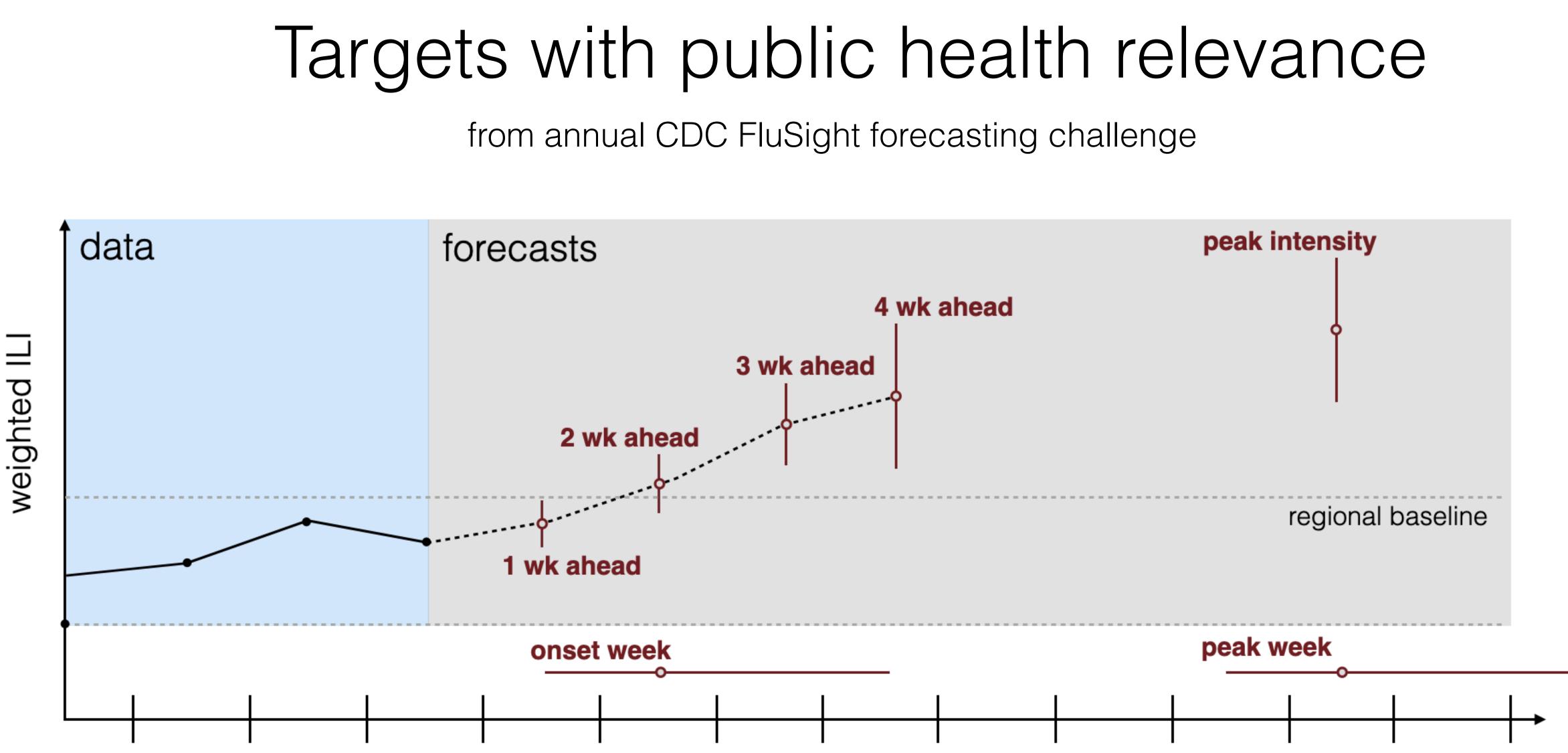
e.g. CDC FluSight challenges: U.S. national, regional, state level. Running annually since 2013.

The % of all outpatient visits with primary complaint of influenza-like illness (ILI), weighted by state population.



2012





Biggerstaff et al. 2016, *BMC Inf Dis*. <u>https://doi.org/10.1186/s12879-016-1669-x</u> McGowan et al. 2019, Sci Rep. https://doi.org/10.1038/s41598-018-36361-9 Lutz et al. 2019. BMC Pub Hlth. https://www.ncbi.nlm.nih.gov/pmc/articles/PMC6902553/

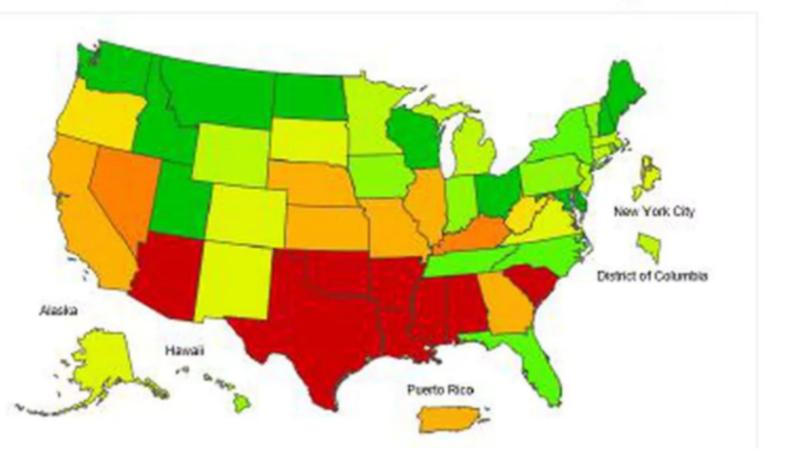


To Your Health

Why this may be a bad flu season, especially around the holidays

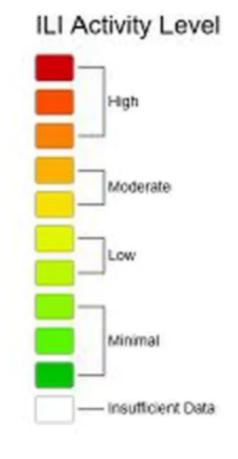
CDC's flu forecasters say there's a 30 percent chance the season will peak around the end of December and a 60 percent chance that the greatest incidence will be by late January, Jernigan said. Generally, flu season peaks near the end of February.

> Influenza-Like Illness (ILI) Activity Level Indicator Determined by Data Reported to ILINet 2017-18 Influenza Season Week 50 ending Dec 16, 2017



The Washington Post

By Lena H. Sun December 22, 2017





Dan Jernigan, Director of Influenza Division, CDC September 2018

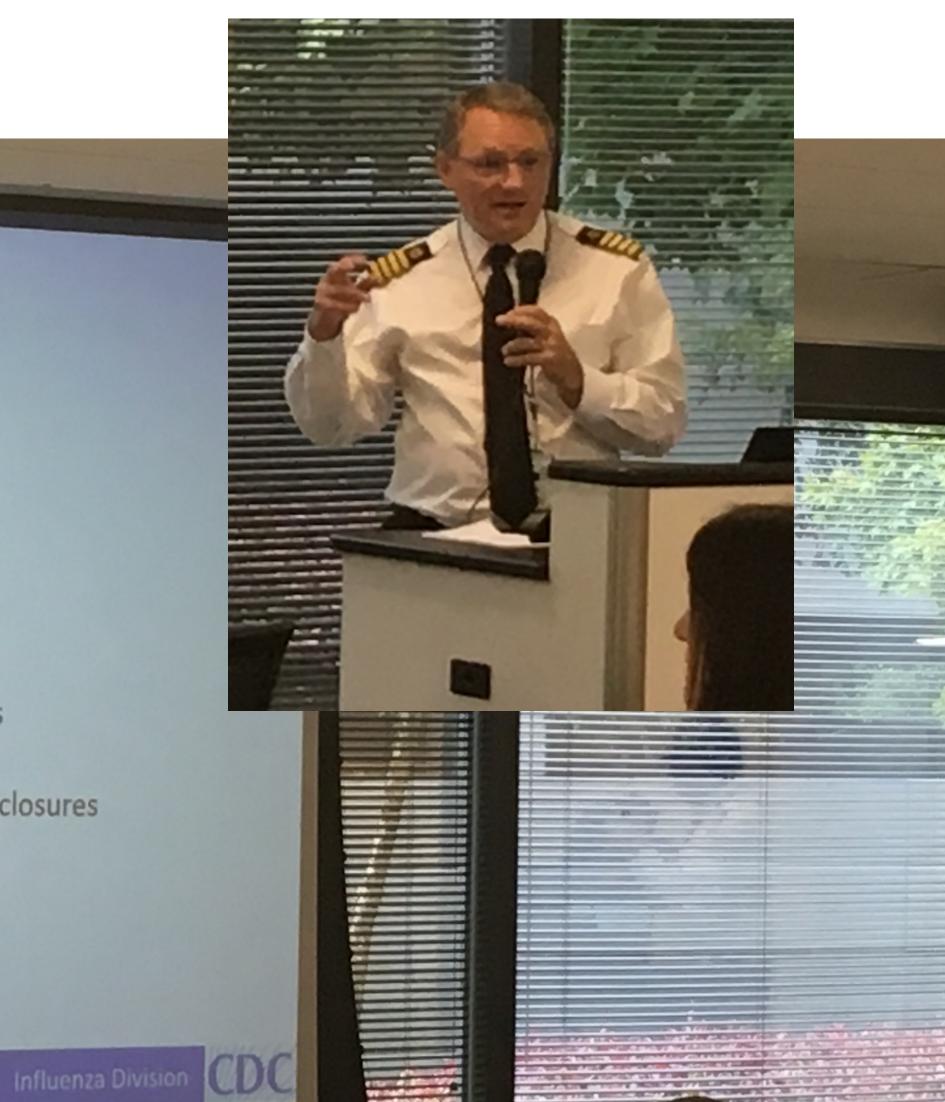
Forecasting Applications

- Informing healthcare providers
 - Outpatient clinic staffing
 - **Emergency** Department staffing and triage
 - Hospital general ward and ICU bed planning
- Informing pharmacies
 - Antiviral and symptom-reducing drug supplies
- Informing parents

 - Push messages on warning signs of severe influenza Improved situational awareness for enhancing flu prevention actions
- Informing Schools
 - Prepare for increased absenteeism and potential for reactive school closures
- Informing Businesses
 - Alert for higher potential for absenteeism or caring for ill children
- Pandemic response
- Improving situational awareness through media

photo credit: Roni Rosenfeld







Model coordination is key

- efforts (flu, Ebola, chikungunya, Zika, dengue, etc...).
- on a single model or team.
- One consistent finding across all efforts:

Flu: Reich et al. 2019, PLOS Comp Bio. https://doi.org/10.1371/journal.pcbi.1007486 Flu: McGowan et al. 2019, *Sci Rep*. <u>https://doi.org/10.1038/s41598-018-36361-9</u> Dengue: Johansson et al. 2019, PNAS. Ebola: Viboud et al. 2018, *Epidemics*. COVID-19: Cramer et al. 2020, *medrxiv*.

There have been numerous government-coordinated outbreak forecasting

• A combination of individual forecasts is pragmatic: it reduces dependency

Combining models into an "ensemble" provides more consistent forecasts than any single model.

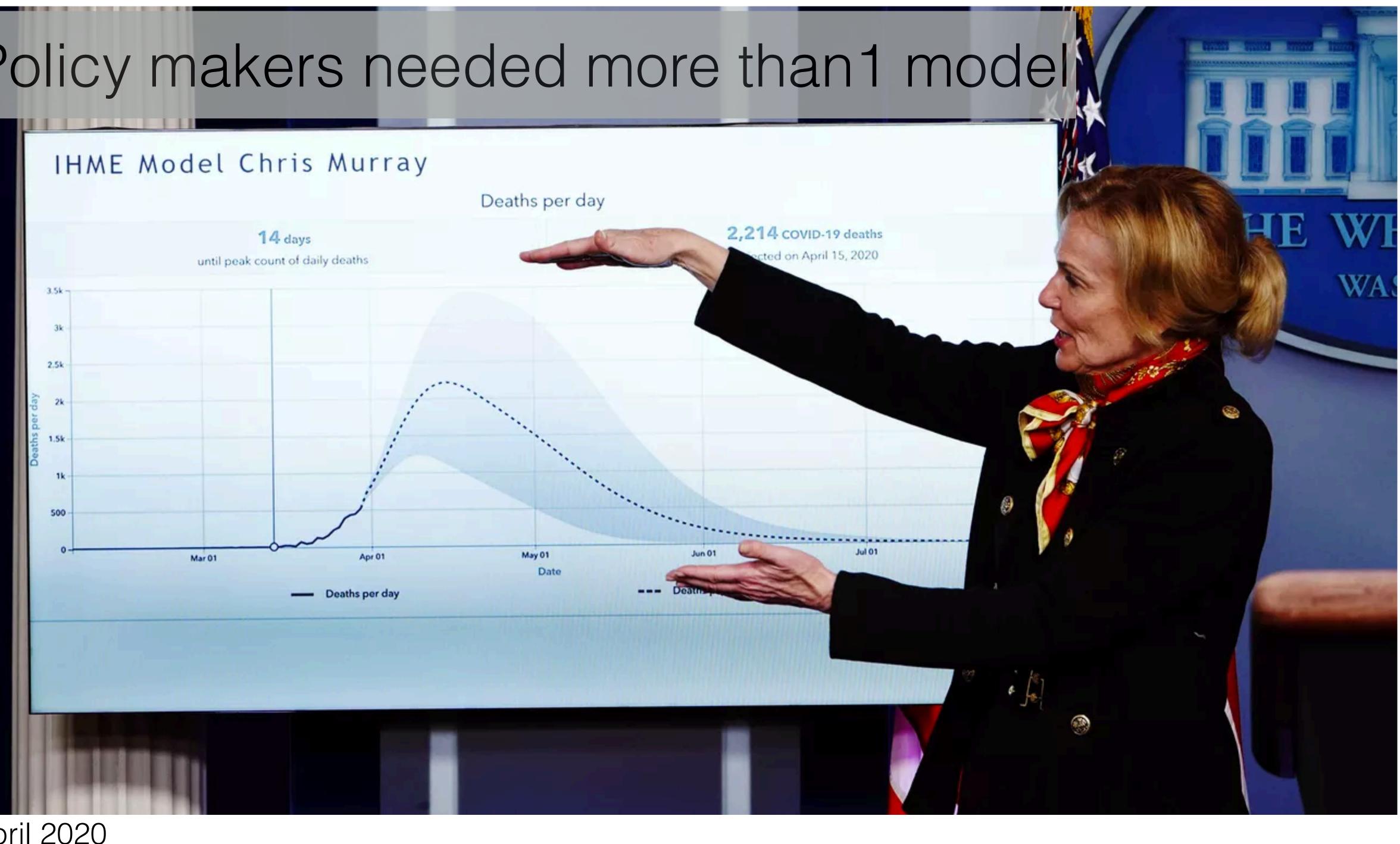
The "Hub" idea is not new

- The idea: coordinated modeling between groups to inform policy and/or develop knowledge about a system.
- Different than a competition: involving coordination between groups and input from policy-makers, often in real-time.

Climate **IDCC** ipcc.ch Ecology ERIES & MARINE ECOSYSTEM isimip.org/about/marine-ecosystems-fisheries/ Space Science Communi MODELING CENTER ccmc.gsfc.nasa.gov



Policy makers needed more than 1 model



early April 2020

Chapter 3: The US COVID-19 Forecast Hub



covid19forecasthub.org Launched April 6, 2020

- about where the pandemic is headed in the next month.
- 2. Assess reliability of forecasts and gain insight into which modeling approaches do well.
- open-science ethos.

Read more: <u>https://covid19forecasthub.org/doc/research/</u>

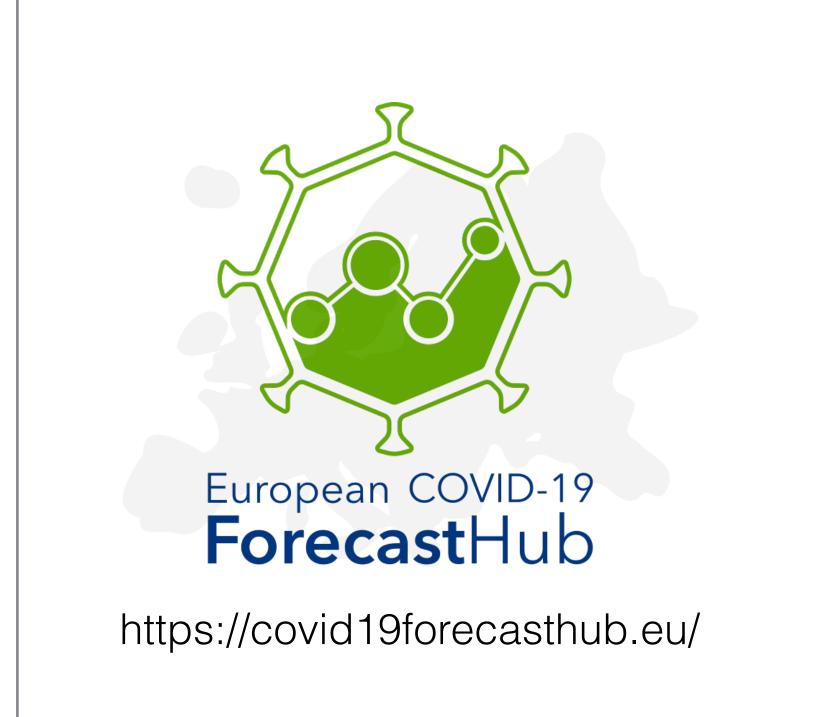
(i)

1. Provide decision-makers and general public with reliable information

3. Create a community of infectious disease modelers underpinned by an







Clones



https://covid19scenariomodelinghub.org/





- groups.
- The Hub builds an ensemble that combines quantile-based predictive distributions from these models for 1 through 4 week ahead forecasts.
- and 71 million unique predictions.

Data on GitHub and on Zoltar. https://github.com/reichlab/covid19-forecast-hub/ https://zoltardata.com/project/44

Numbers

 Each week the Forecast Hub receives forecasts of weekly incident cases, hospitalizations and deaths in the US due to COVID-19 from dozens of

• To date, we have curated data from 105 models: over 4,900 submissions



Data from the COVID-19 Forecast Hub are shared directly with the CDC, and published on the CDC website weekly.

https://www.cdc.gov/coronavirus/2019-ncov/covid-data/mathematical-modeling.html



COVID-19 Forecasts: Deaths

Updated Nov. 19, 2020 Print



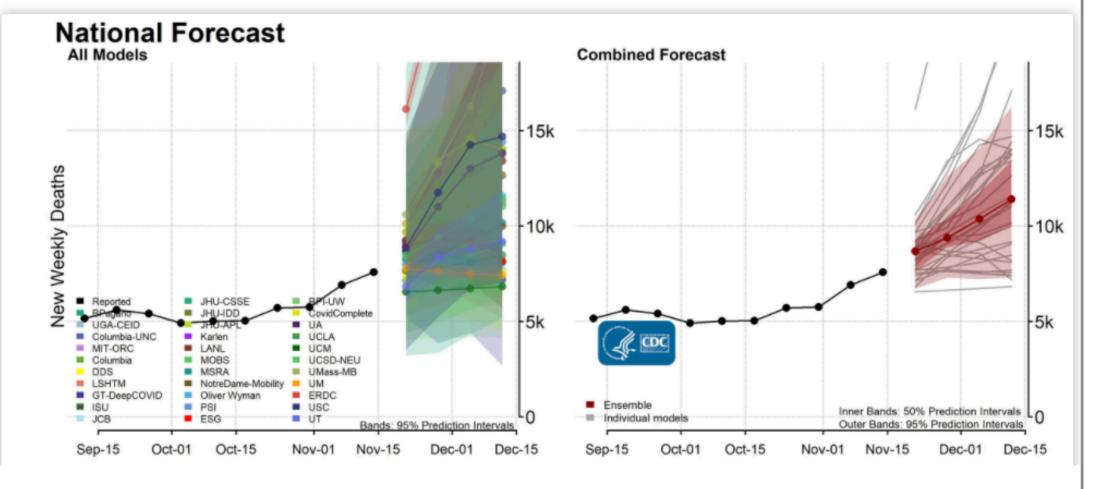
Interpretation of Forecasts of New and Total Deaths

 This week CDC received forecasts of COVID-19 deaths over the next 4 weeks from 36 modeling groups that were included in the ensemble forecast. Of the 36 groups, 33 provided forecasts for both new and total deaths, two groups forecasted total deaths only, and one forecasted new death only.

This week's national <u>ensemble forecast</u> predicts that the number of newly reported COVID-19 deaths will likely increase over the next four weeks, with 7,300 to 16,000 new deaths likely to be reported in the week ending December 12, 2020. The national ensemble predicts that a total of 276,000 to 298,000 COVID-19 deaths will be reported by this date.

• The state- and territory-level ensemble forecasts predict that over the next 4 weeks, the number of newly reported deaths per week will likely increase in 36 jurisdictions, which are indicated in the forecast plots below. Trends in numbers of future reported deaths are uncertain or predicted to remain stable in the other states and territories.

National Forecast



On This Page

National Forecast State Forecasts Ensemble Forecast Forecast Assumptions

Ensemble in use by government officials

100 days



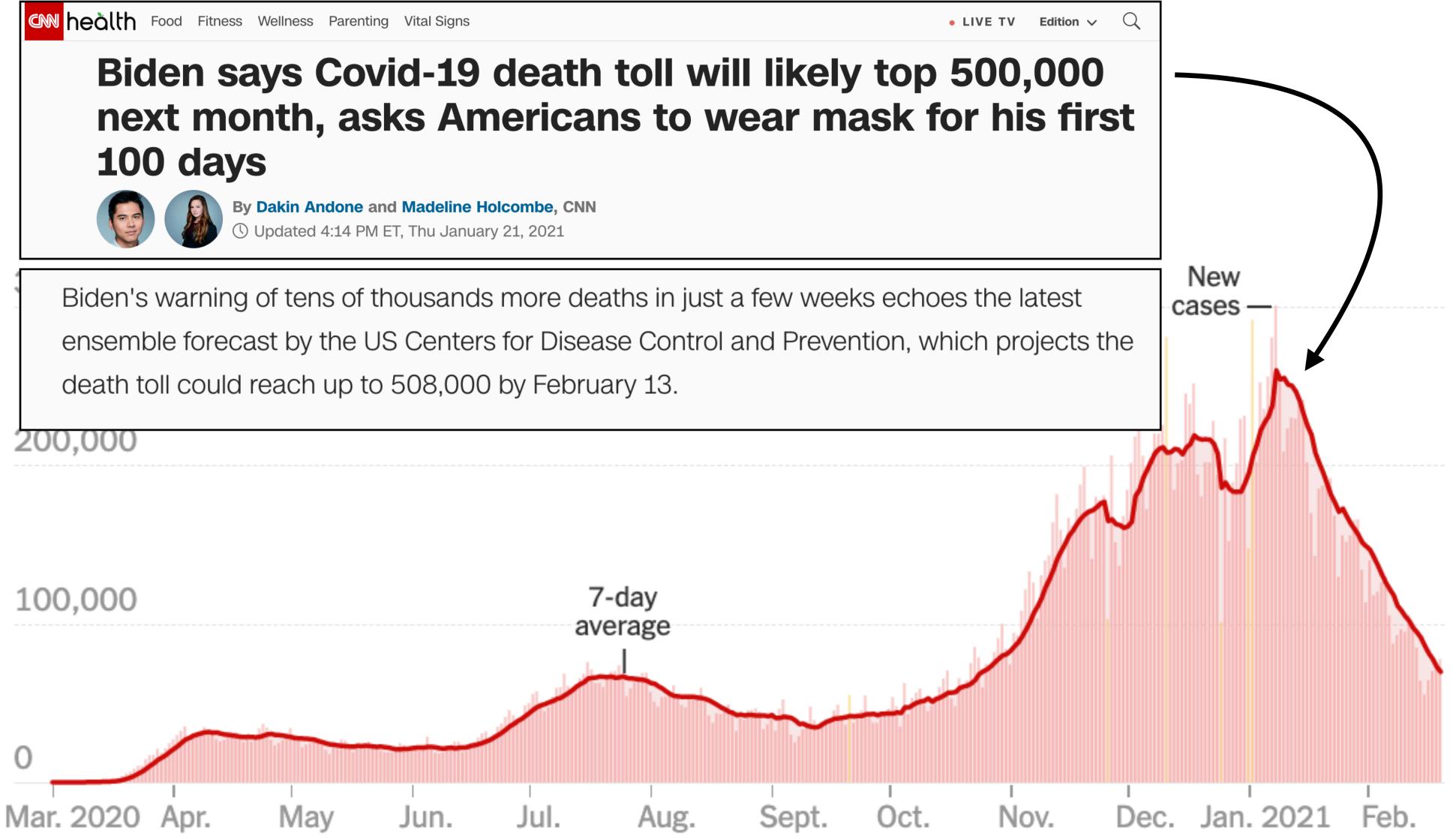
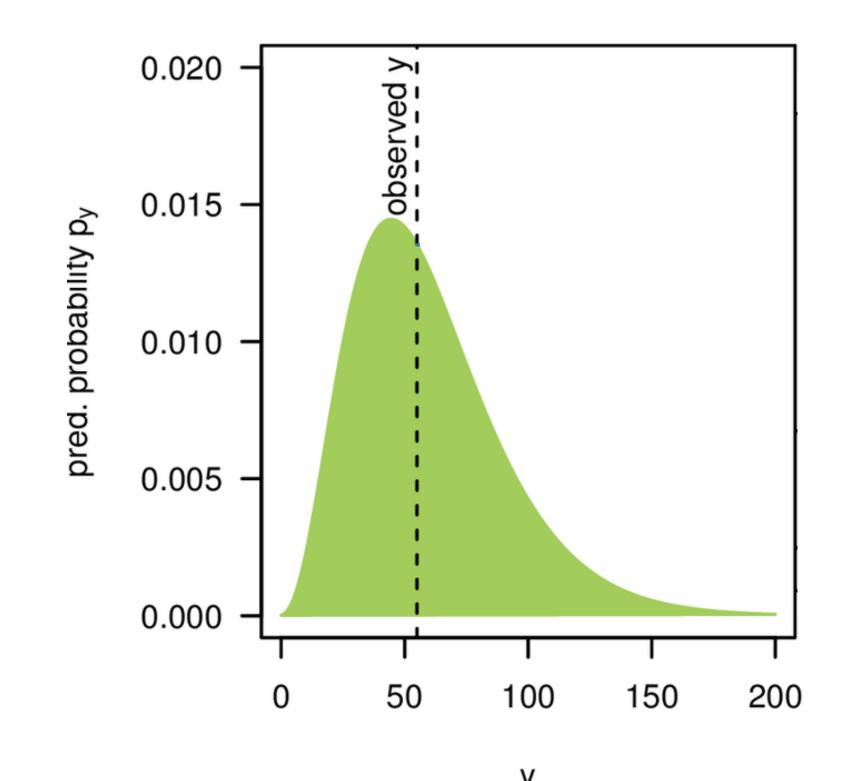


image credit: NY Times

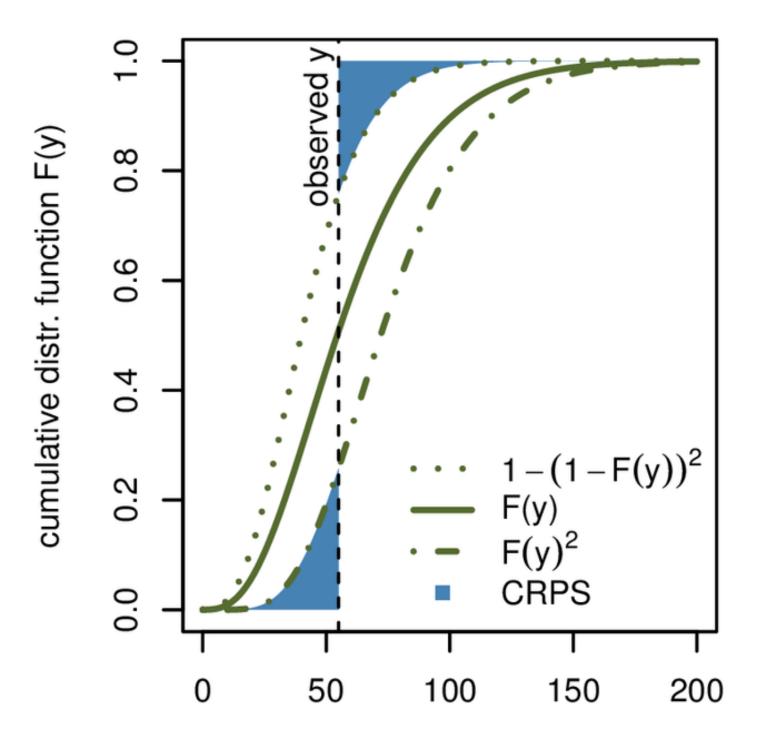
Evaluating forecast accuracy (1)

1. Weighted Interval Score (WIS): a score rewarding both accuracy and precision.



Based on the submission format of forecasts, we developed the WIS which is an approximation to the commonly used Continuous Rank Probability Score (CRPS), and equivalent to the commonly used "pinball loss" in machine learning. Lower scores are better.

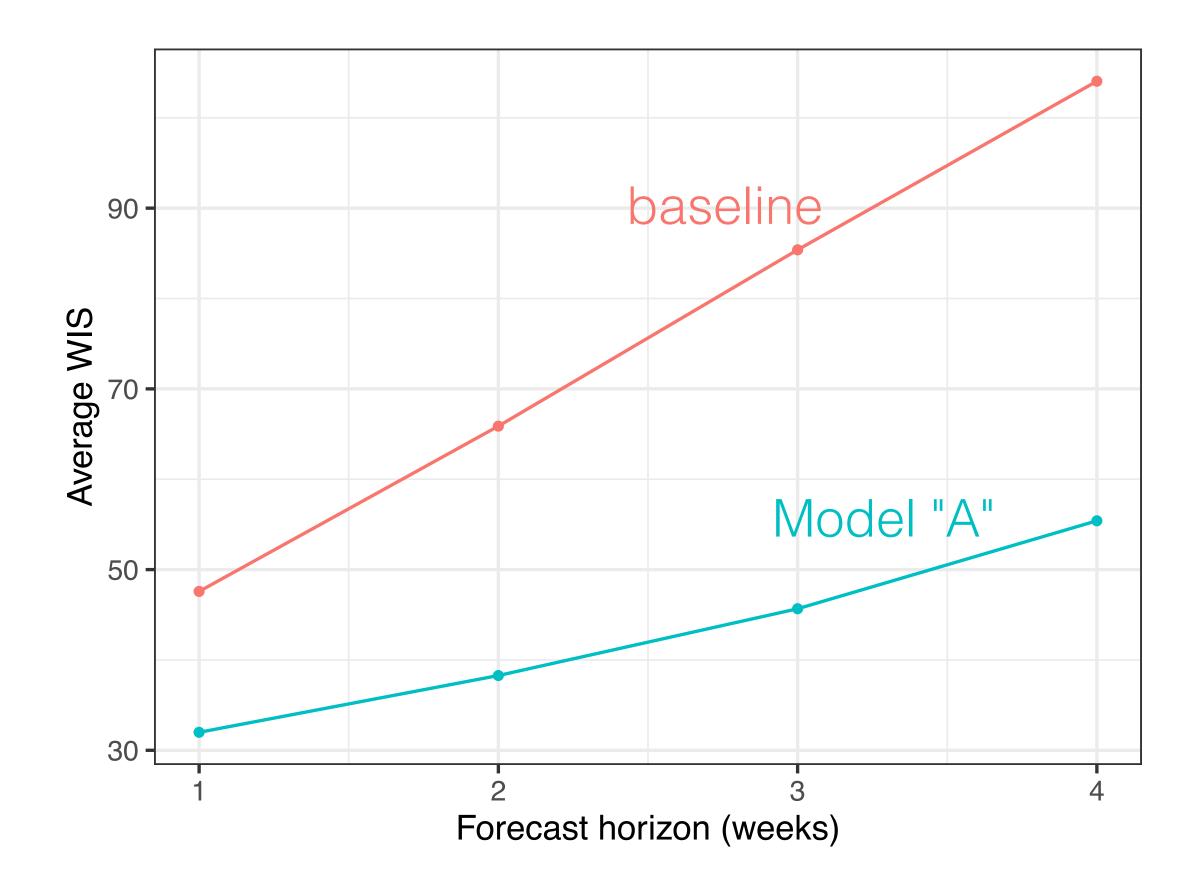
slide adapted from Bracher et al (2021). PLOS Comp Bio. DOI:10.1371/journal.pcbi.1008618



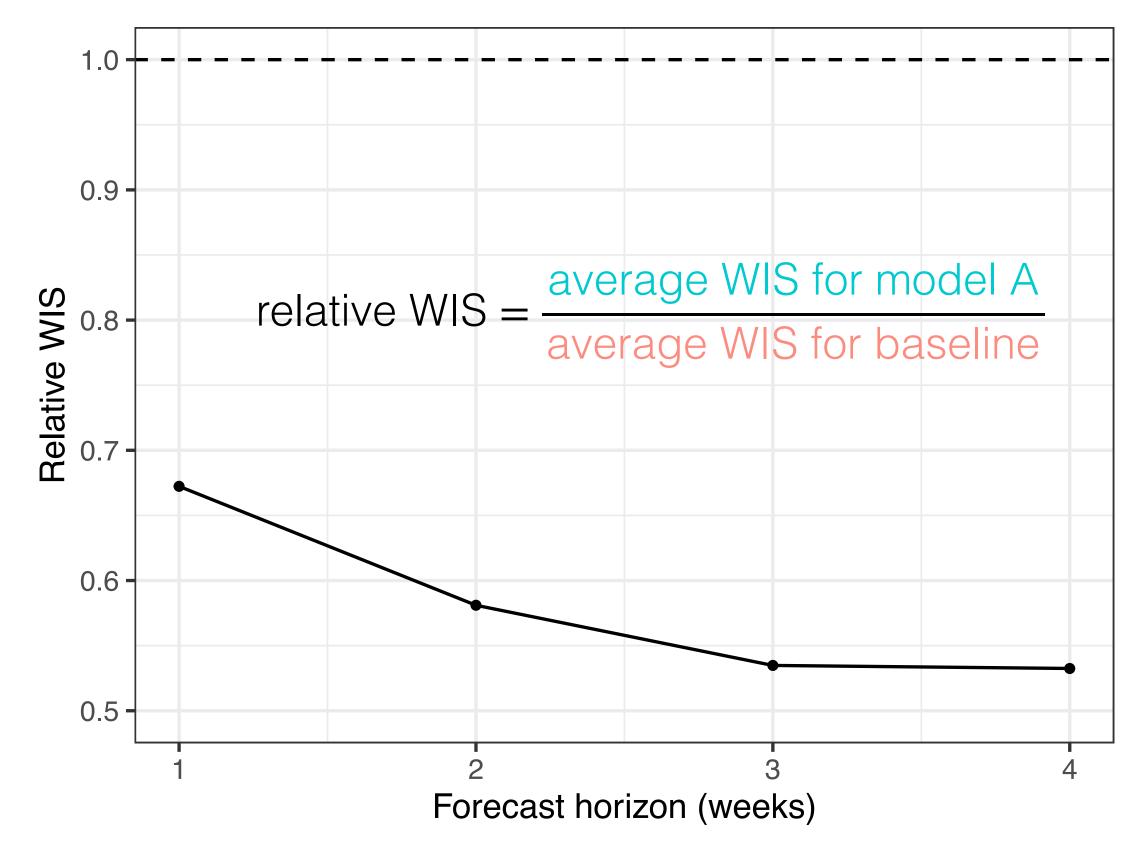


Evaluating forecast accuracy (1a)

1a. Relative Weighted Interval Score (Relative WIS): how accurate is a model relative to a naïve baseline?

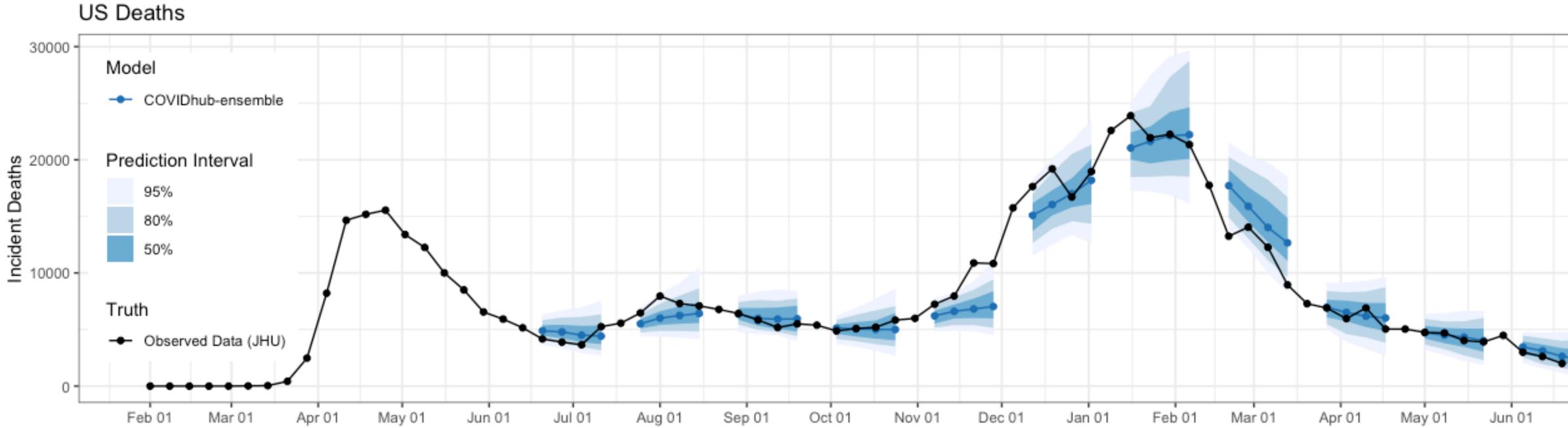


Relative WIS lower than 1 means the forecasts were better than the baseline.



Evaluating forecast accuracy (2)

2. Prediction interval coverage: when you say something has a 50% chance of occurring does it really happen with that frequency?



With millions (!!) of observations across different weeks and locations, we can develop a good sense of how "reliable" the models are.



-		

Jul 01

- and disease transmission models."
- network."
- models for time-varying dynamics, models for partial/noisy observations of confirmed cases and deaths."
- <u>UT-Mobility</u>: "For each US state, we use local data from mobile-phone GPS traces made available by [SafeGraph] to quantify the changing impact of social-distancing measures on 'flattening the curve.' "
- rate on various detailed syndromic, demographic, mobility and clinical data."
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- specific regularization scheme that increases the **coupling between regions**"
- features. No assumptions are made regarding reopening or governmental interventions."

• IHME-CurveFit: "hybrid modeling approach to generate our forecasts, which incorporates elements of statistical

• MOBS-GLEAM COVID: "The GLEAM framework is based on a metapopulation approach in which the world is divided into geographical subpopulations. Human mobility between subpopulations is represented on a

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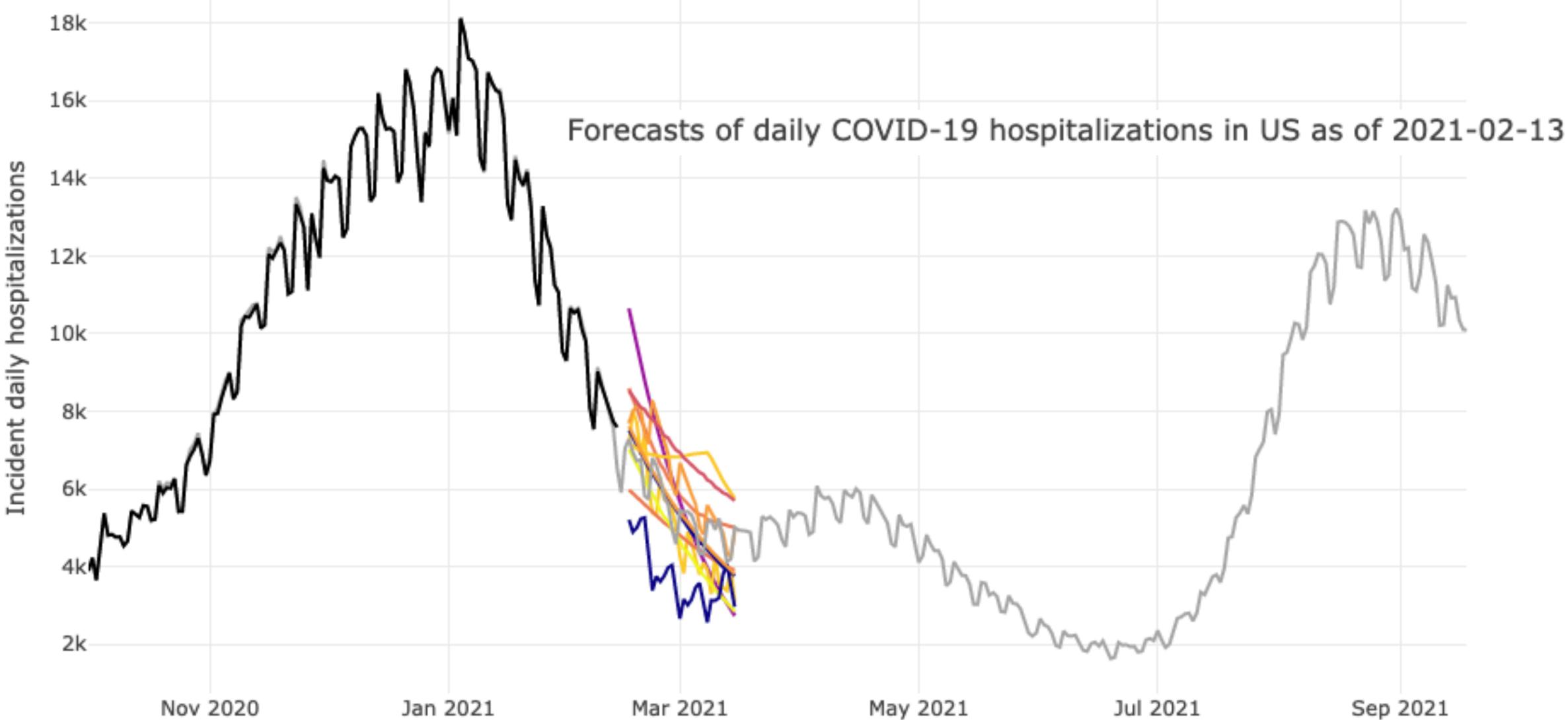
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Forecasts often have made reasonable statements

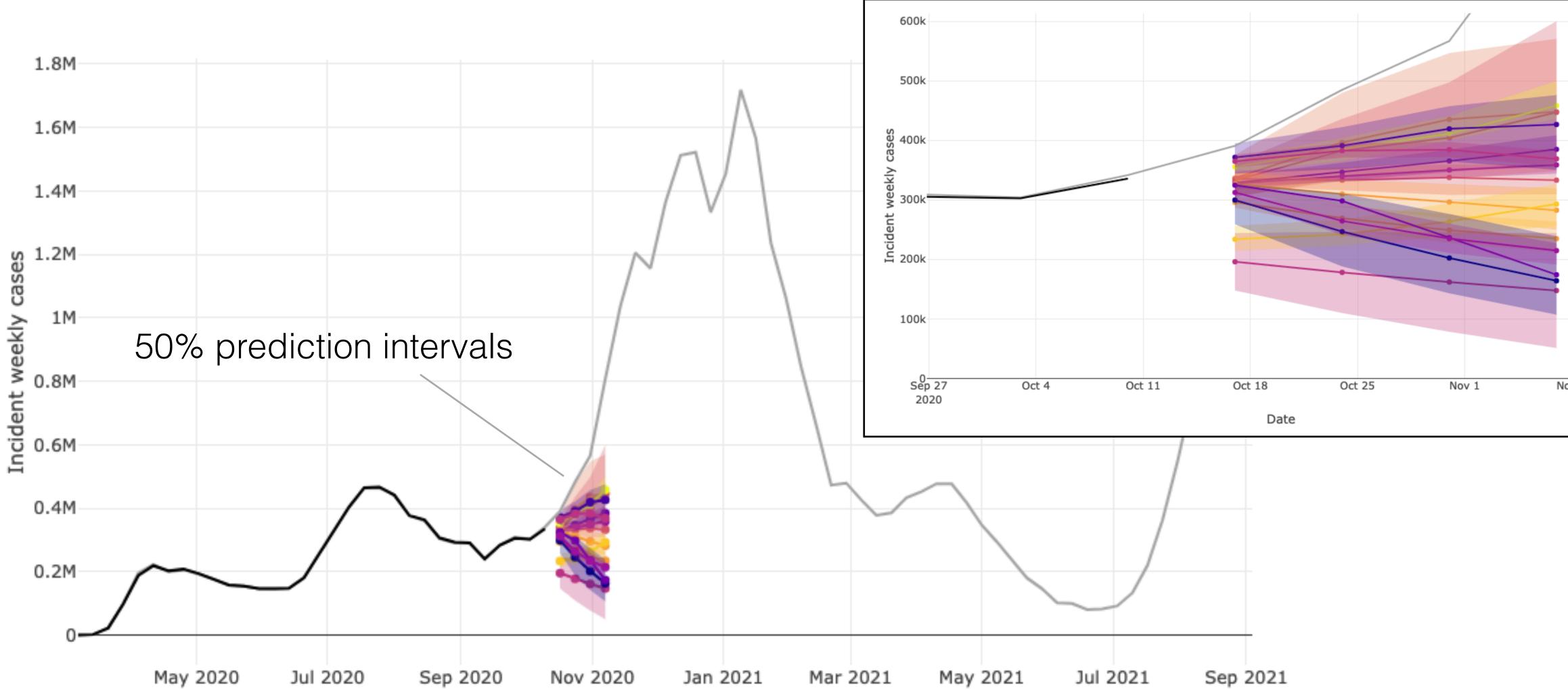


especially during times where a stable trend continues



Forecasts have missed change-points

Forecasts of weekly COVID-19 cases in US as of 2020-10-10



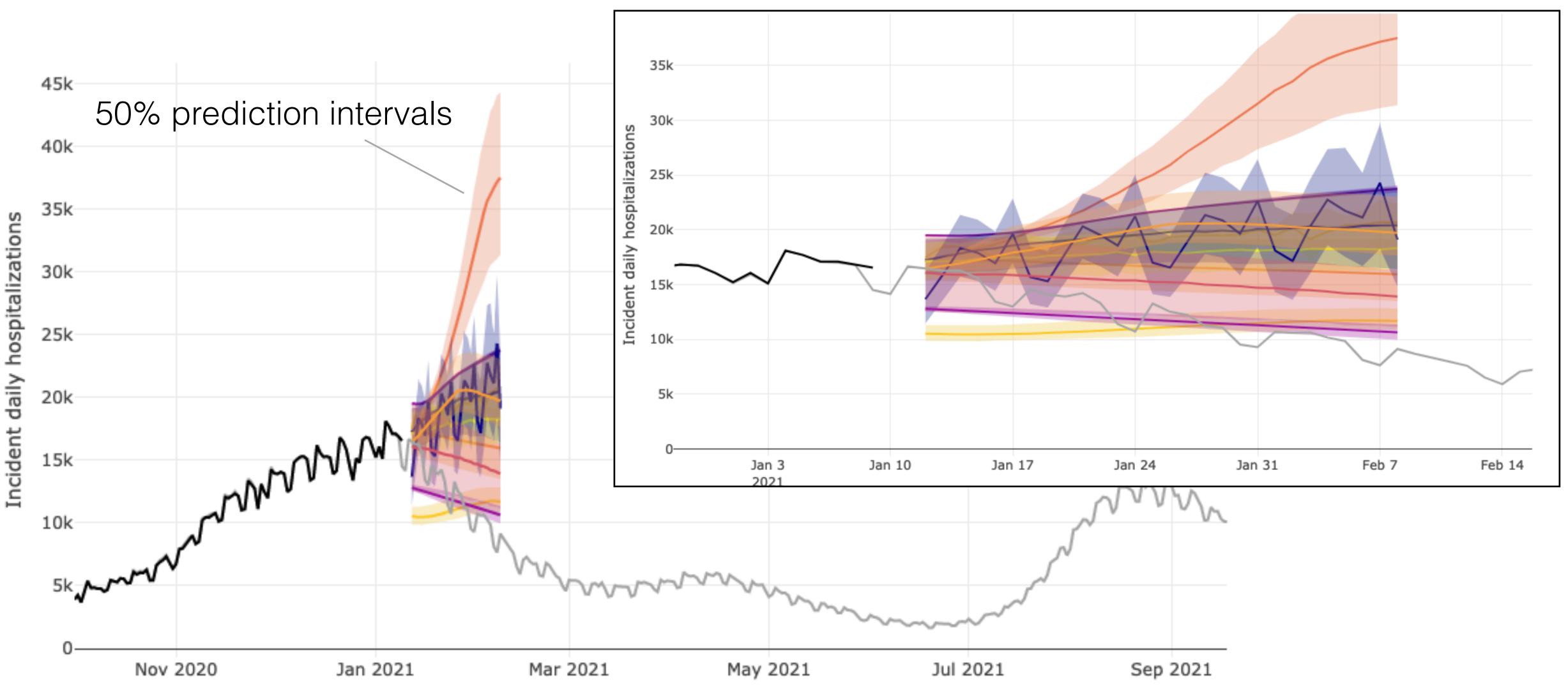
especially for case forecasts

ov 8

Forecasts have missed change-points

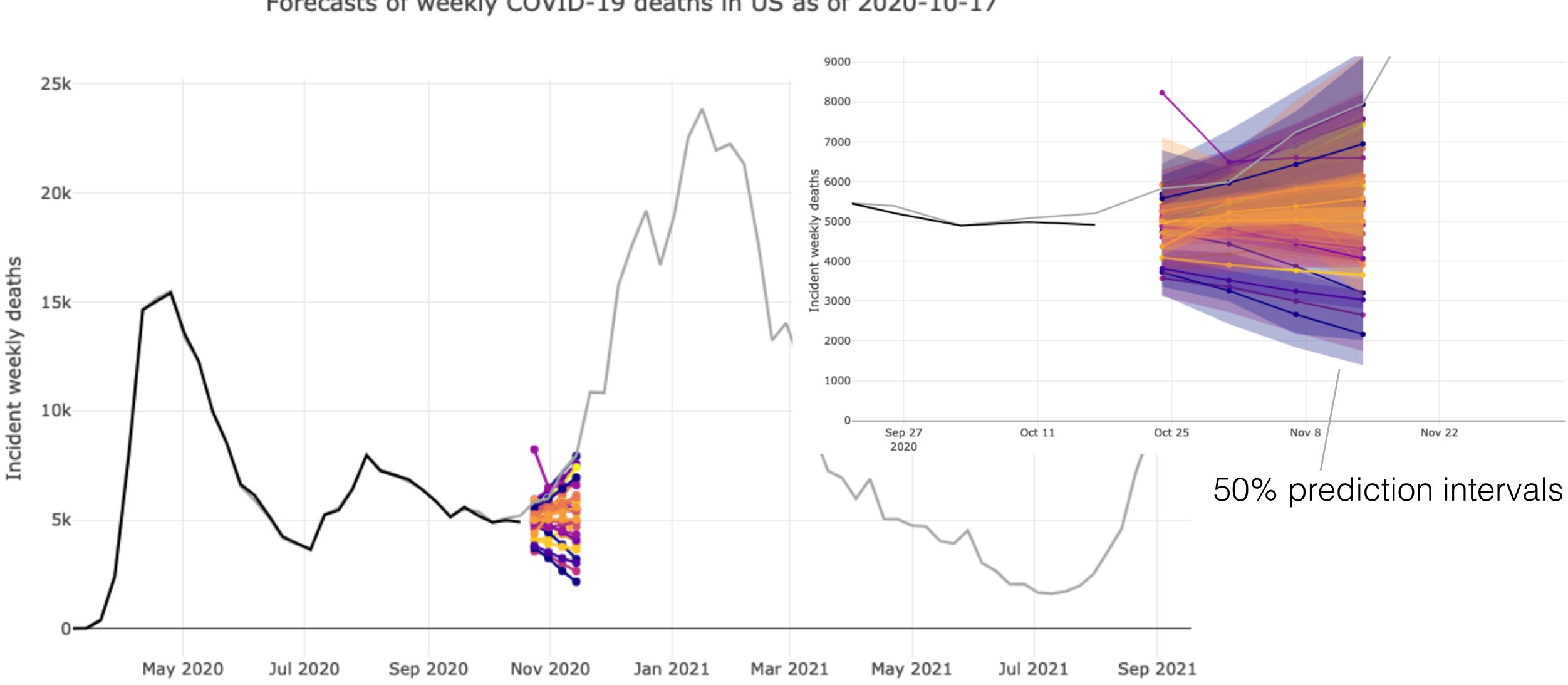
also for hospitalization forecasts

Forecasts of daily COVID-19 hospitalizations in US as of 2021-01-09



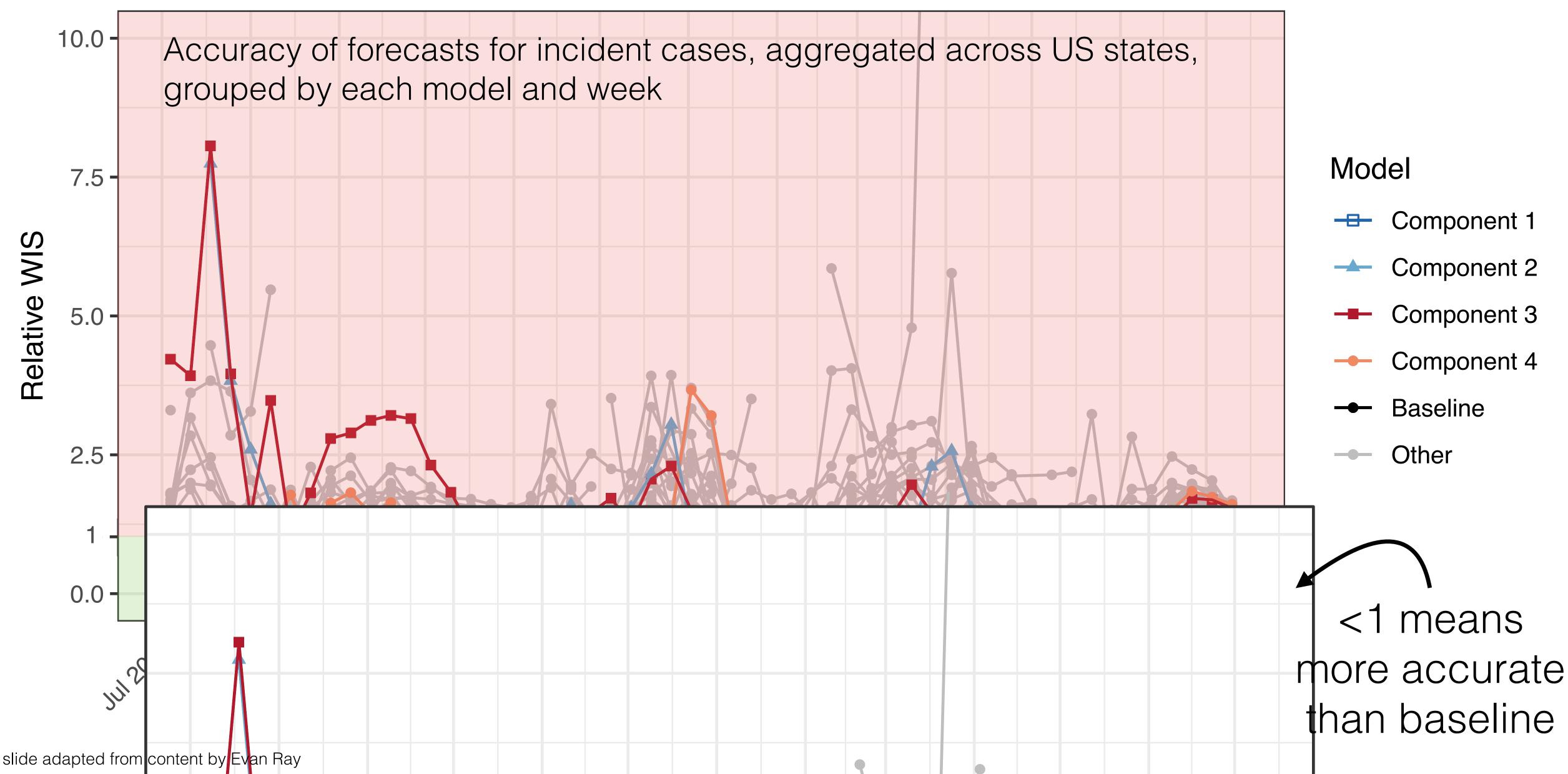
Forecasts have missed change-points

Forecasts of weekly COVID-19 deaths in US as of 2020-10-17



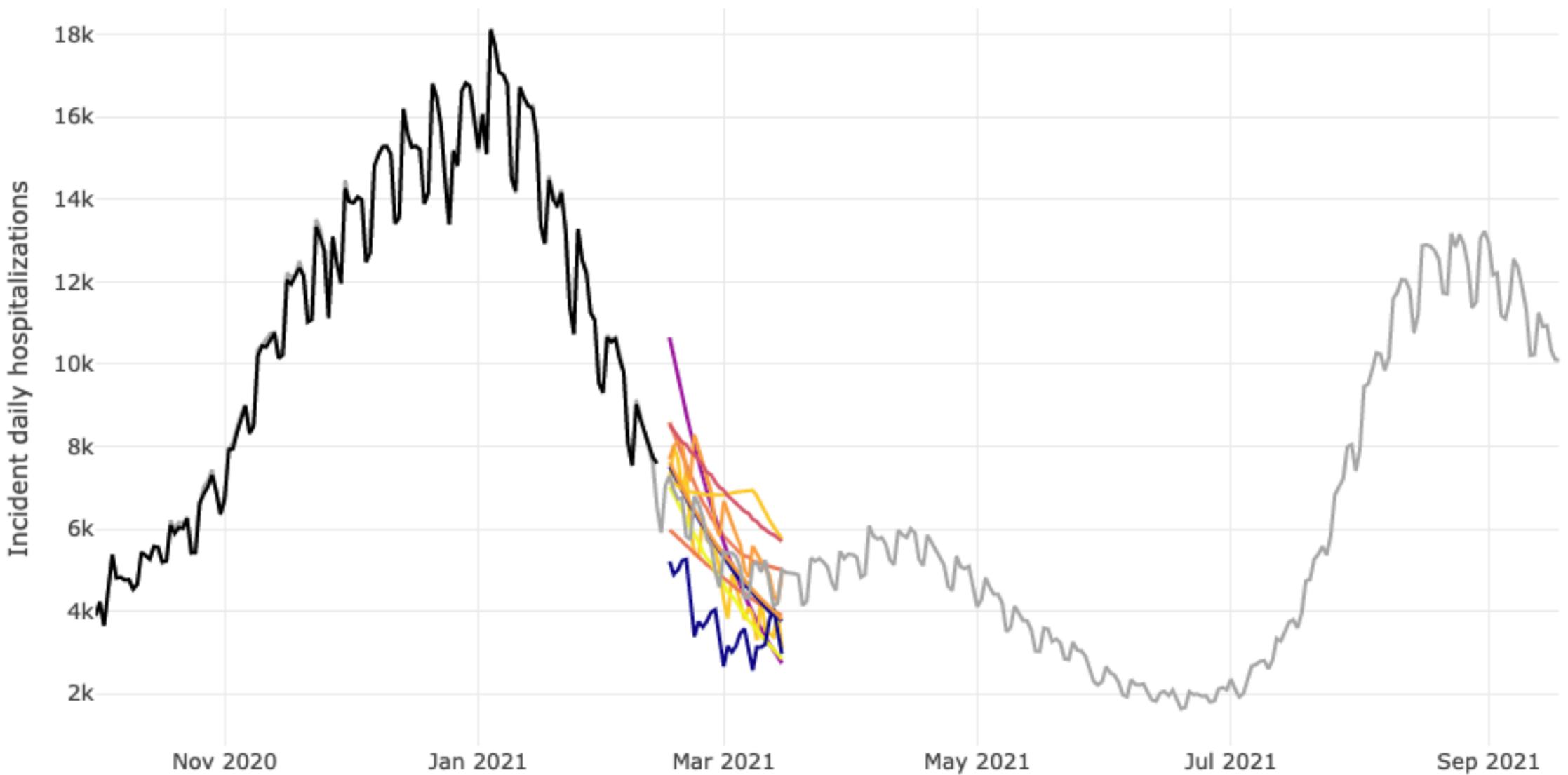
and for deaths as well

Model performance changes over time





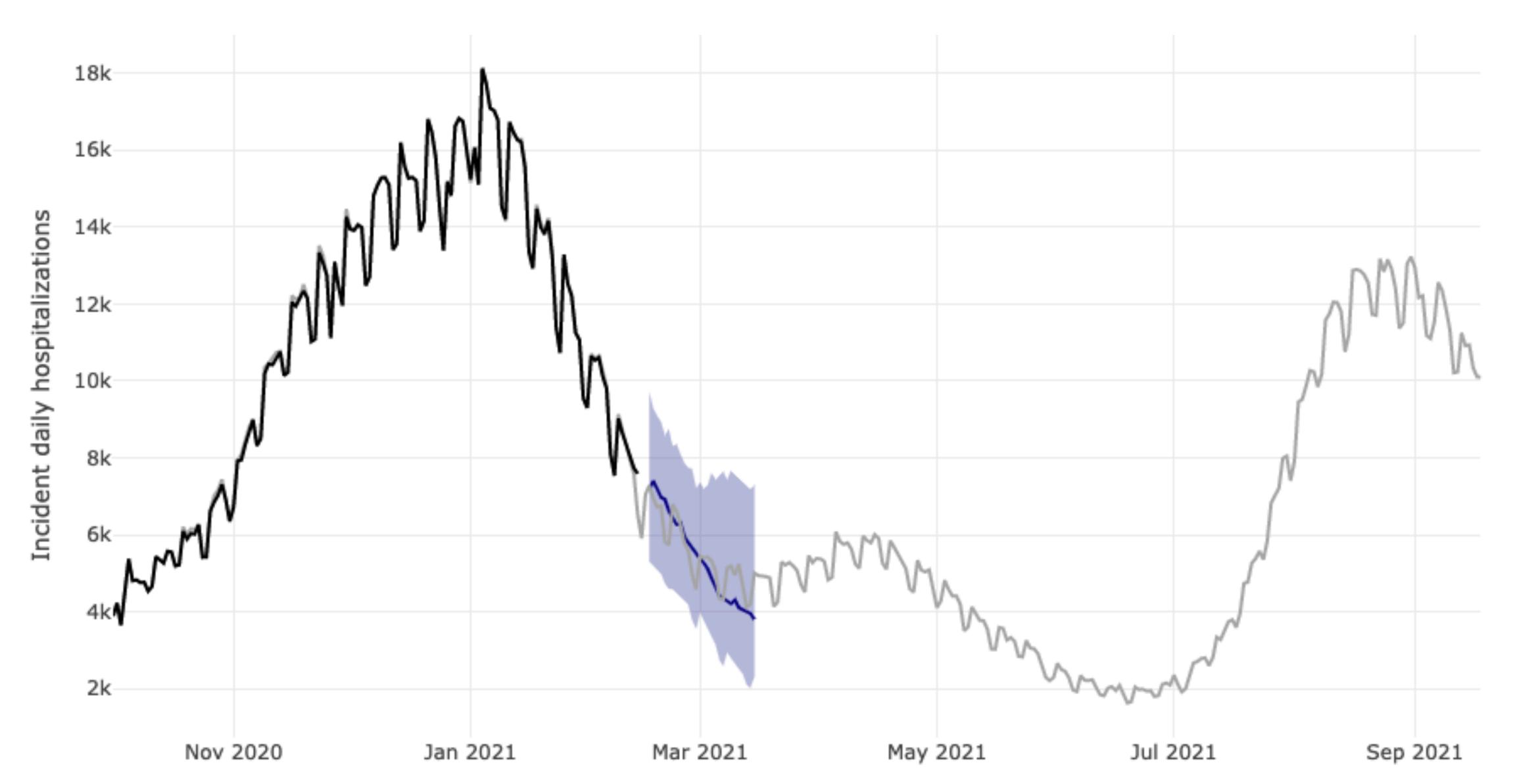
Ensemble model to the rescue?



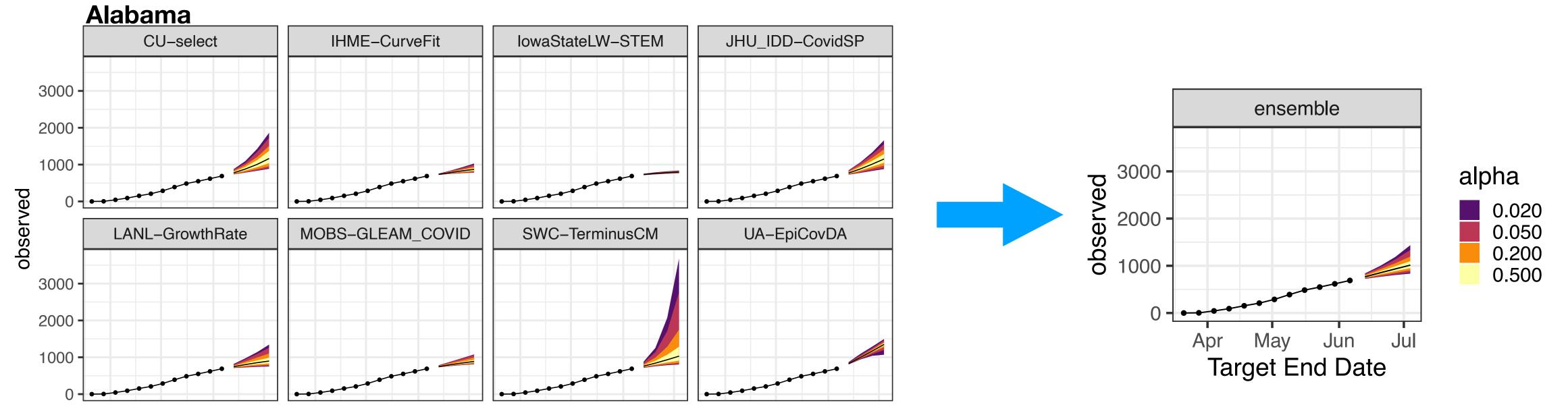
Nov 2020

Jan 2021

Ensemble model to the rescue?



Building the Ensemble: View 1



K=23 (or 7) quantiles of a predictive distribution: $\widehat{P}(Y \le q_{s,t,h,1}^m) = 0.01, \ \widehat{P}(Y \le q_{s,t,h,2}^m) = 0.025.$ The pre

Limits of a 98

level:

slide adapted from content by Evan Ray

• For each combination of spatial unit s, time point t, and forecast horizon h, teams are required to submit

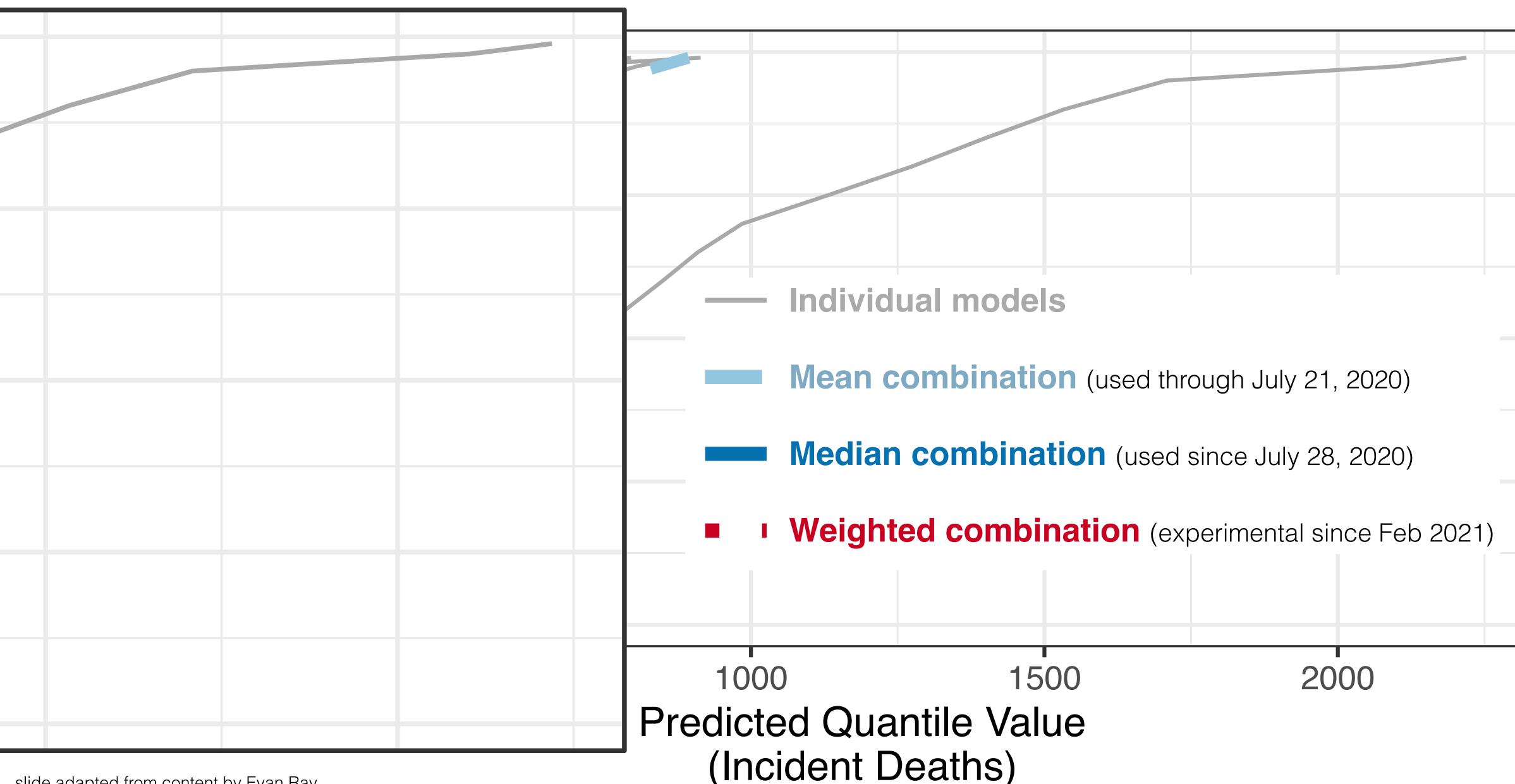
edictive median

$$P(Y \le q_{s,t,h,12}^m) = 0.5, \dots, \widehat{P}(Y \le q_{s,t,h,23}^m) = 0.99$$

 $P(Y \le q_{s,t,h,23}^m) = 0.99$
 $P(Y \le q_{s,t,h,23}^m) = 0.99$

• The predictive quantiles for the ensemble are a combination of component predictions at each quantile $q_{s,t,h,k} = f(q_{s,t,h,k}^1, ..., q_{s,t,h,k}^M)$ for each k = 1,...,23

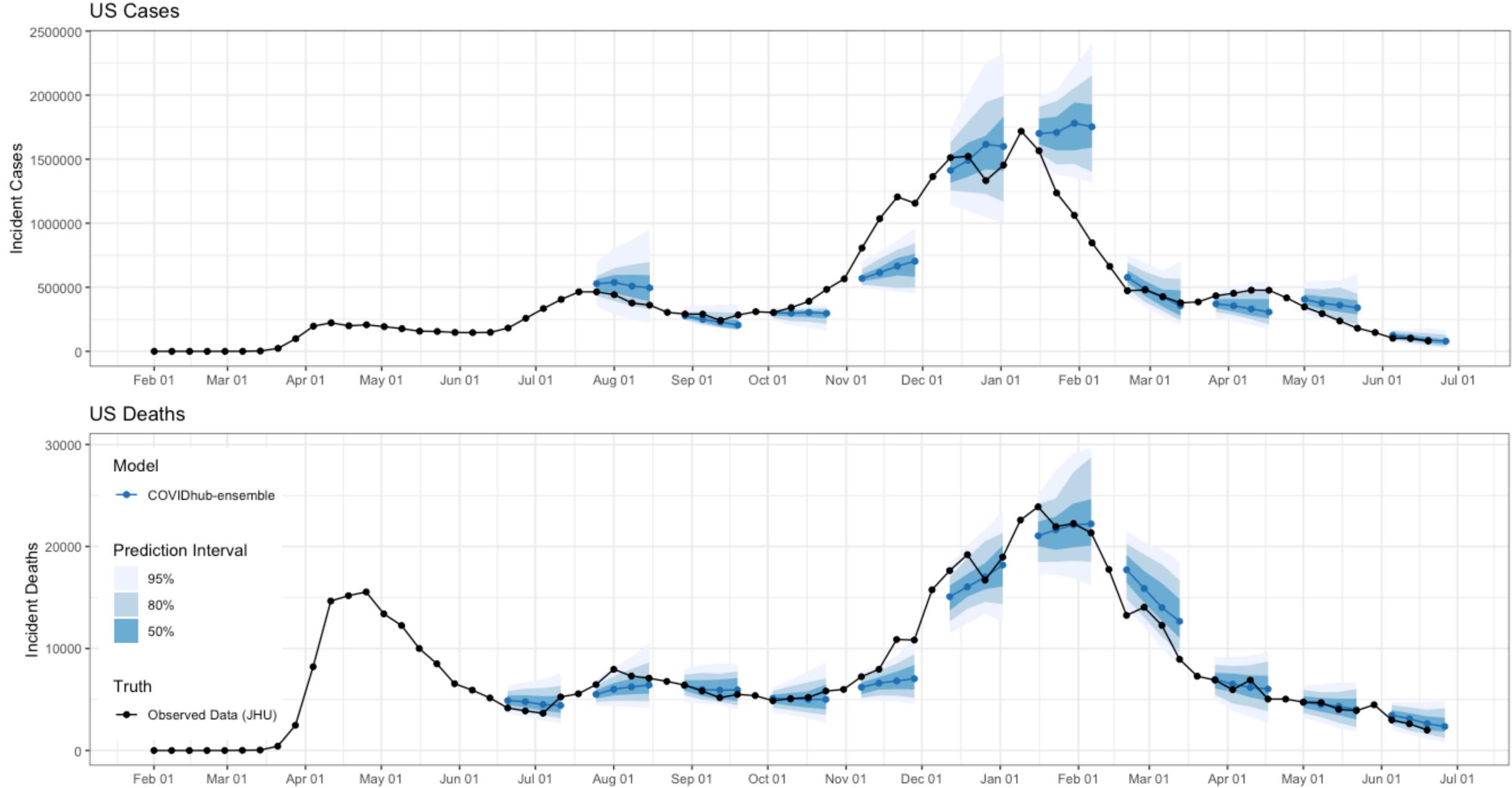
Building an Ensemble: View 2



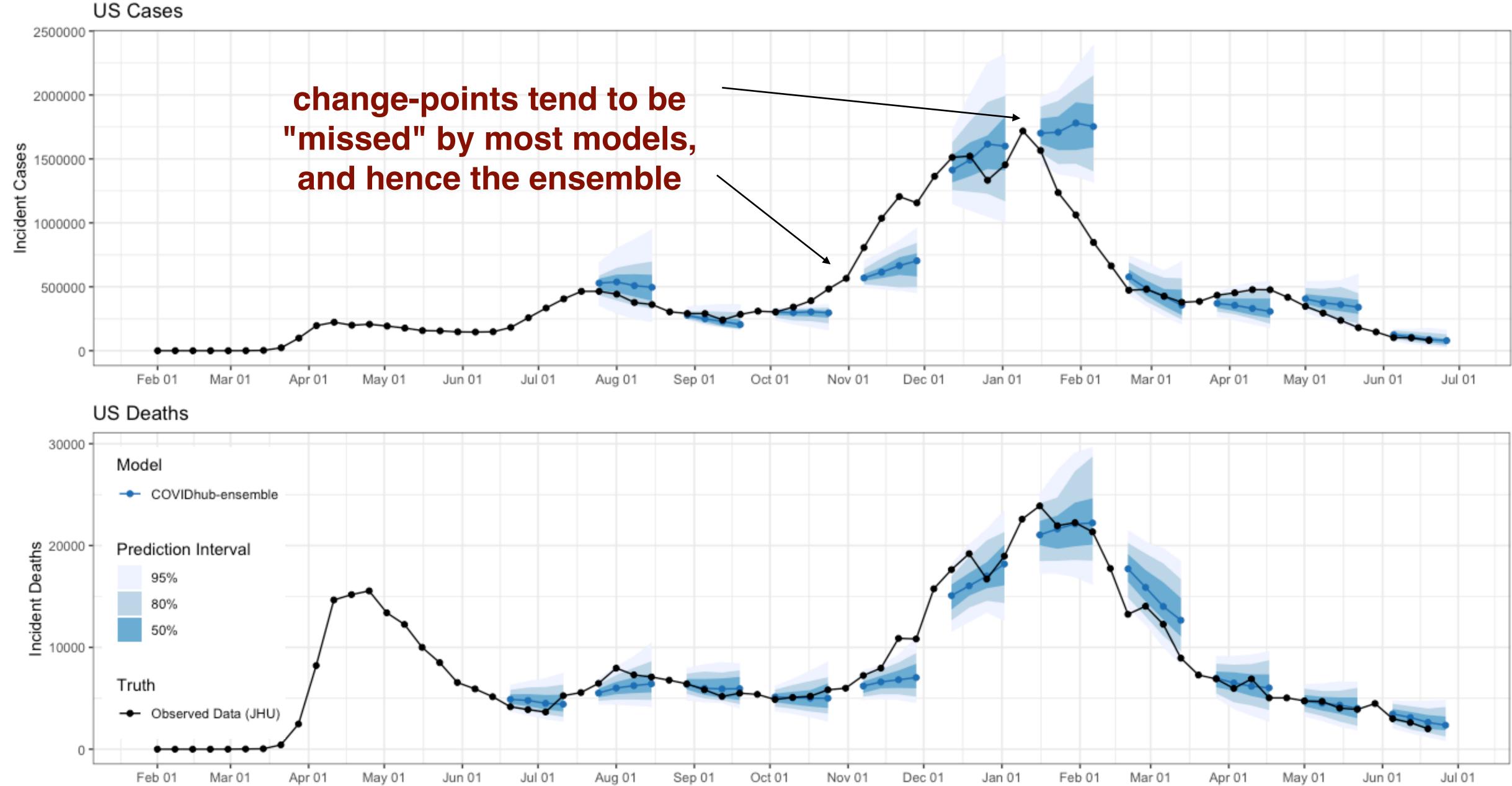
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Ensemble forecasts over time



Ensemble forecasts over time



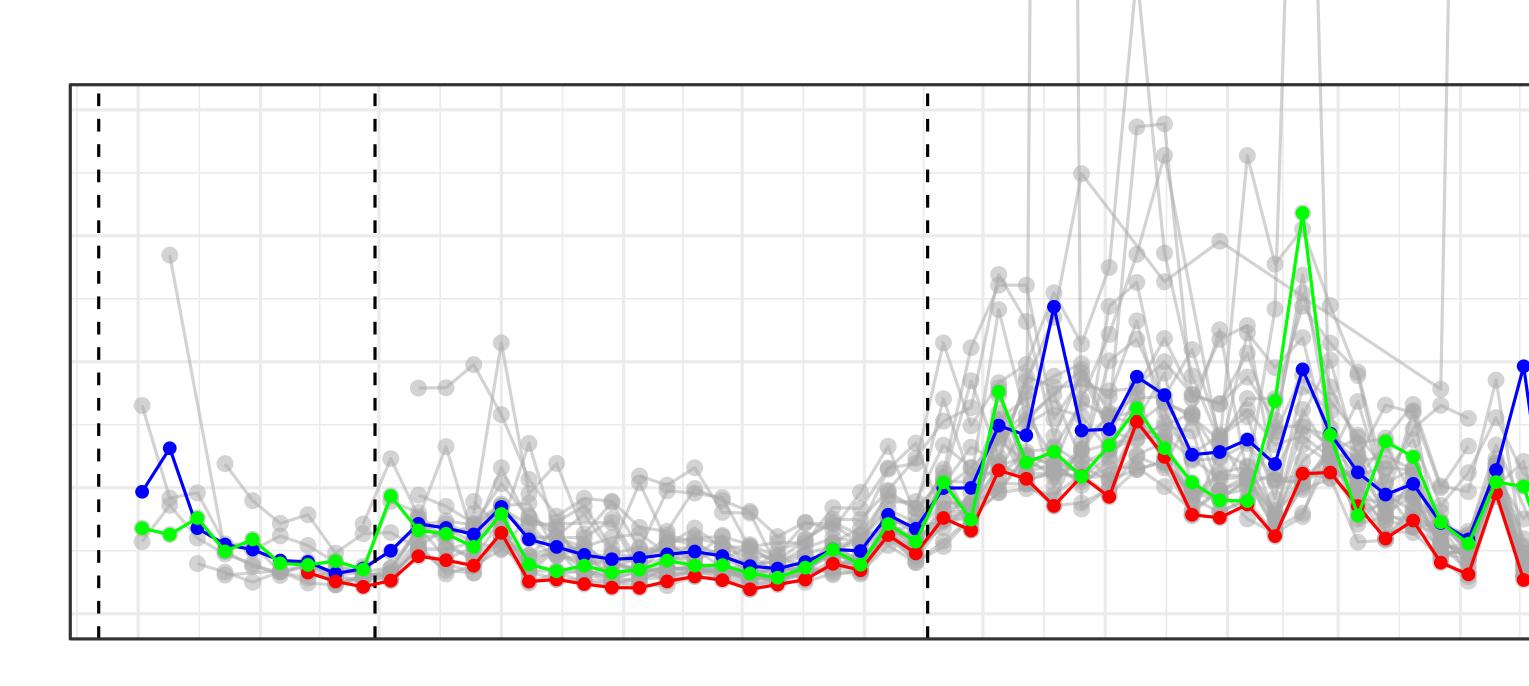
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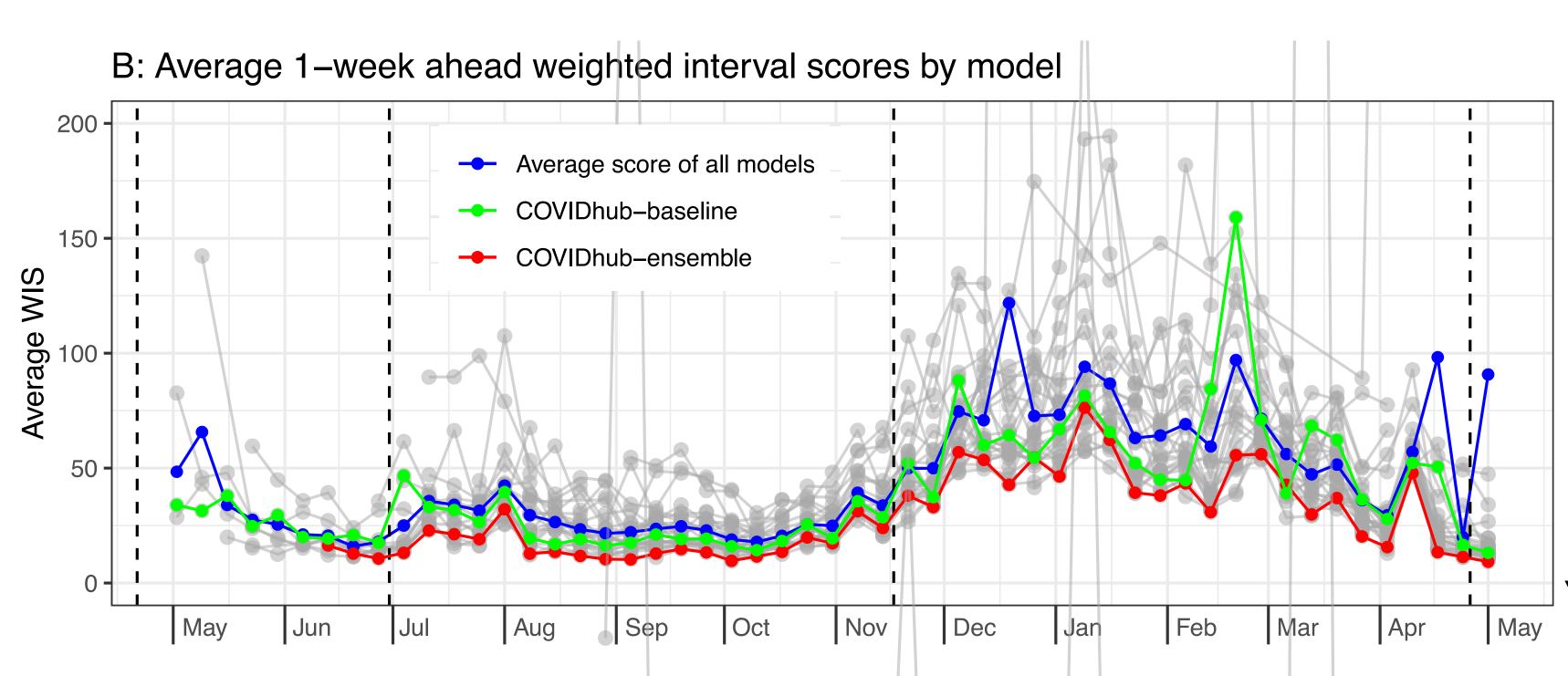
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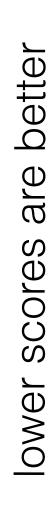
Incident deaths in Legan 10000 -

5000 -



Forecast accuracy over time





Ensembles have shown top performance Metrics computed using forecasts from the last 6 months...

Forecasts of COVID-19 cases

model	rel. WIS	95% cov.
COVIDhub-ensemble	0.90	0.72
USC-SI_kJalpha	0.95	0.44
CU-select	0.99	0.53
		0

- 24 individual models for cases*
- 3 models (13%) better than baseline at 3 & 4 weeks ahead

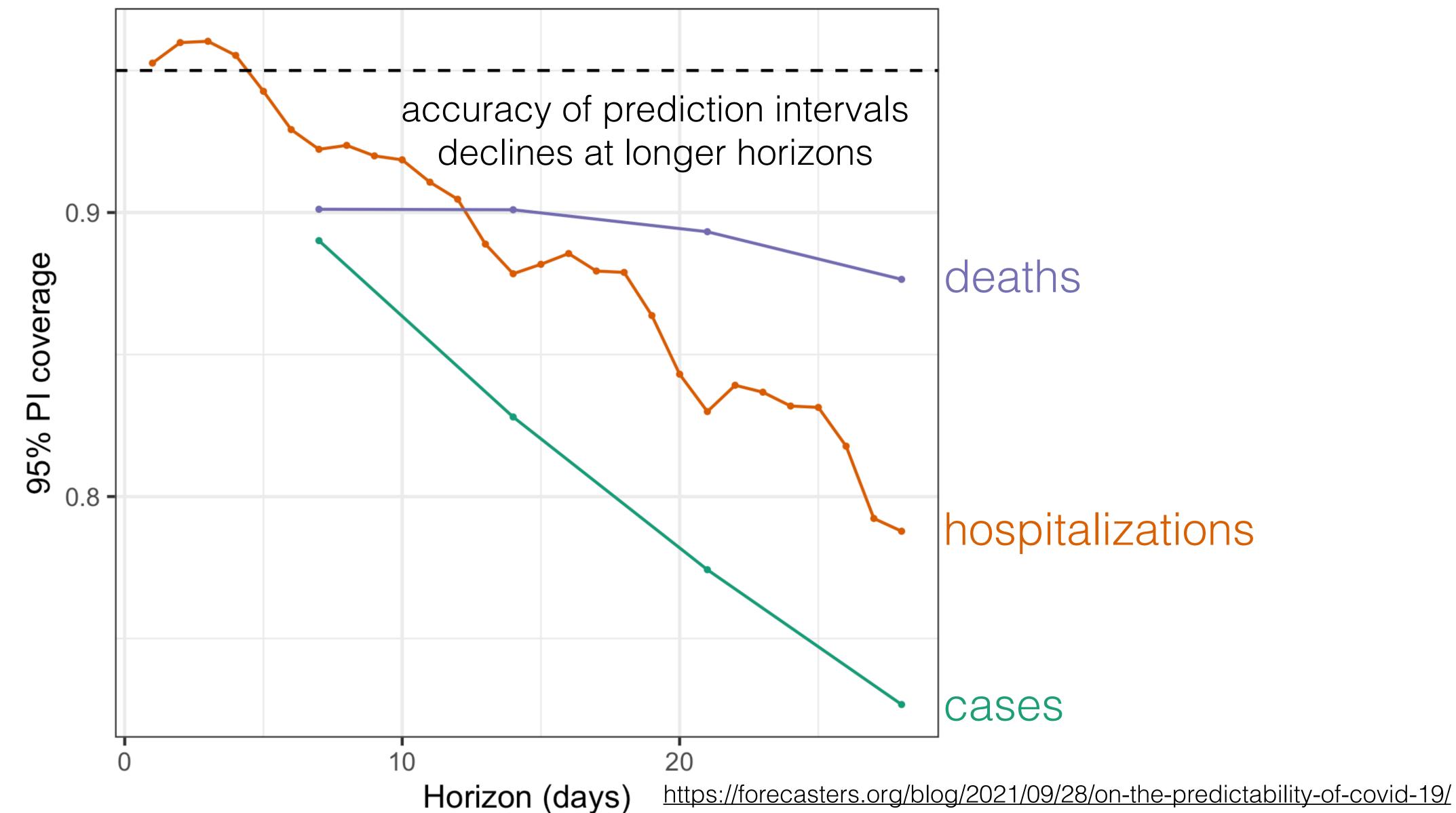
* Models had to have submitted forecasts for at least 13 of the past 26 weeks. More scores at: <u>https://covid19forecasthub.org/eval-reports/?state=US&week=2021-09-22</u>

Forecasts of COVID-19 deaths

model	rel. WIS	95% cov.
COVIDhub-ensemble	0.54	0.94
CMU-TimeSeries	0.57	0.91
JHU_CSSE-DECOM	0.59	0.76
IHME-CurveFit	0.60	0.52
SteveMcConnell-CovidComplete	0.61	0.75
MOBS-GLEAM_COVID	0.61	0.78
UMass-MechBayes	0.62	0.90

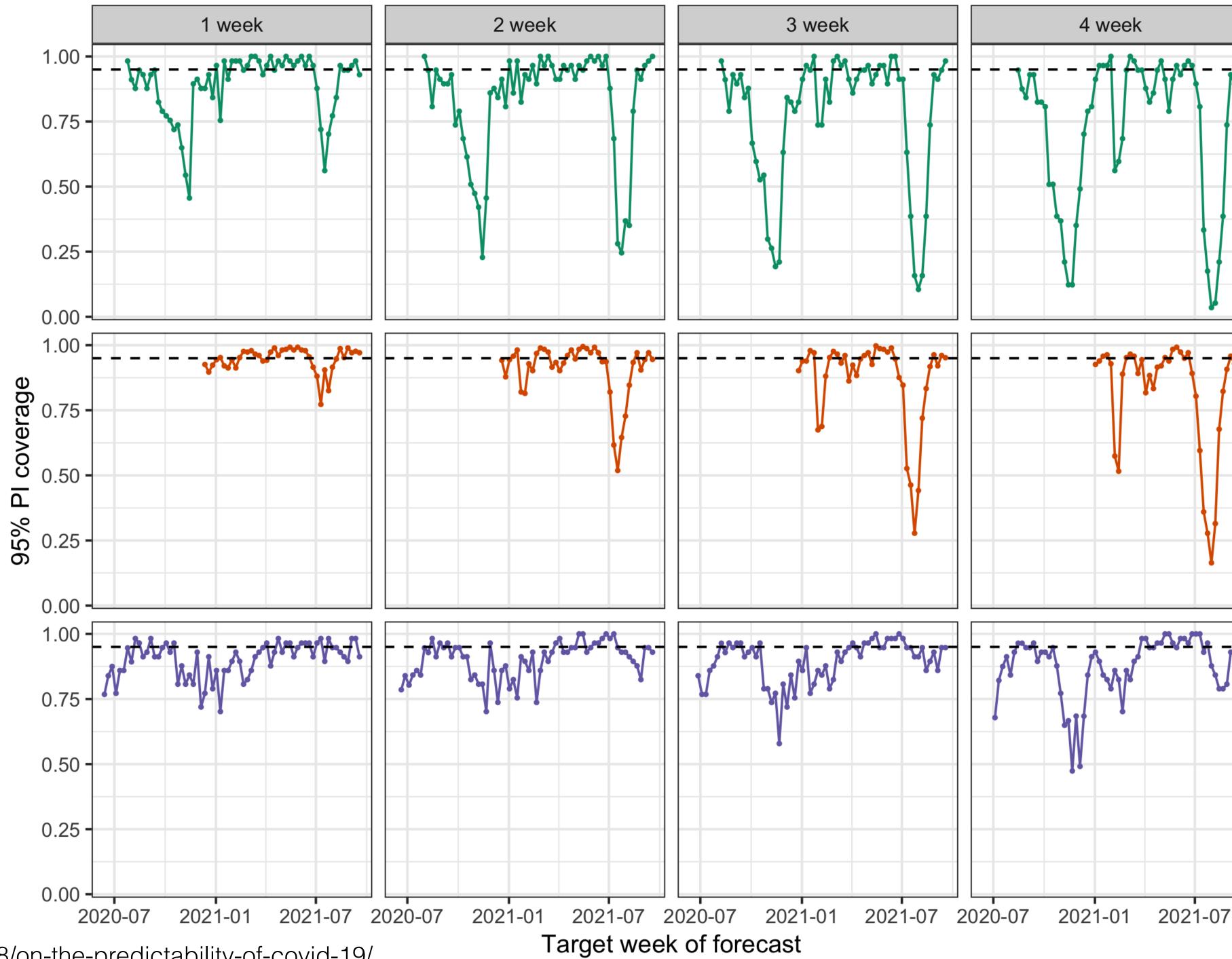
- 33 individual models for deaths*
- 24 models (73%) better than baseline at 4 weeks ahead

Overall, ensemble accuracy varies by target and error increases as we look further into the future

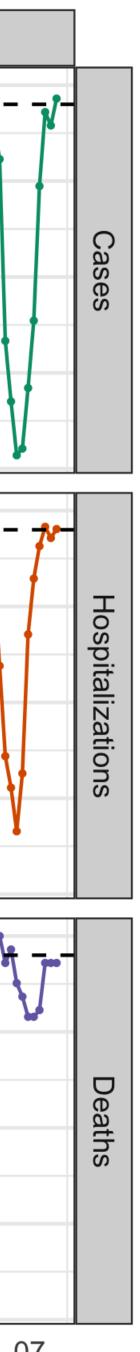




Interval coverage over time reveals systemic problems



https://forecasters.org/blog/2021/09/28/on-the-predictability-of-covid-19/

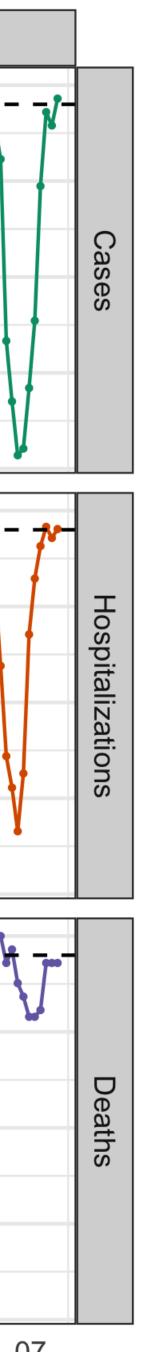


Interval coverage over time reveals systemic problems

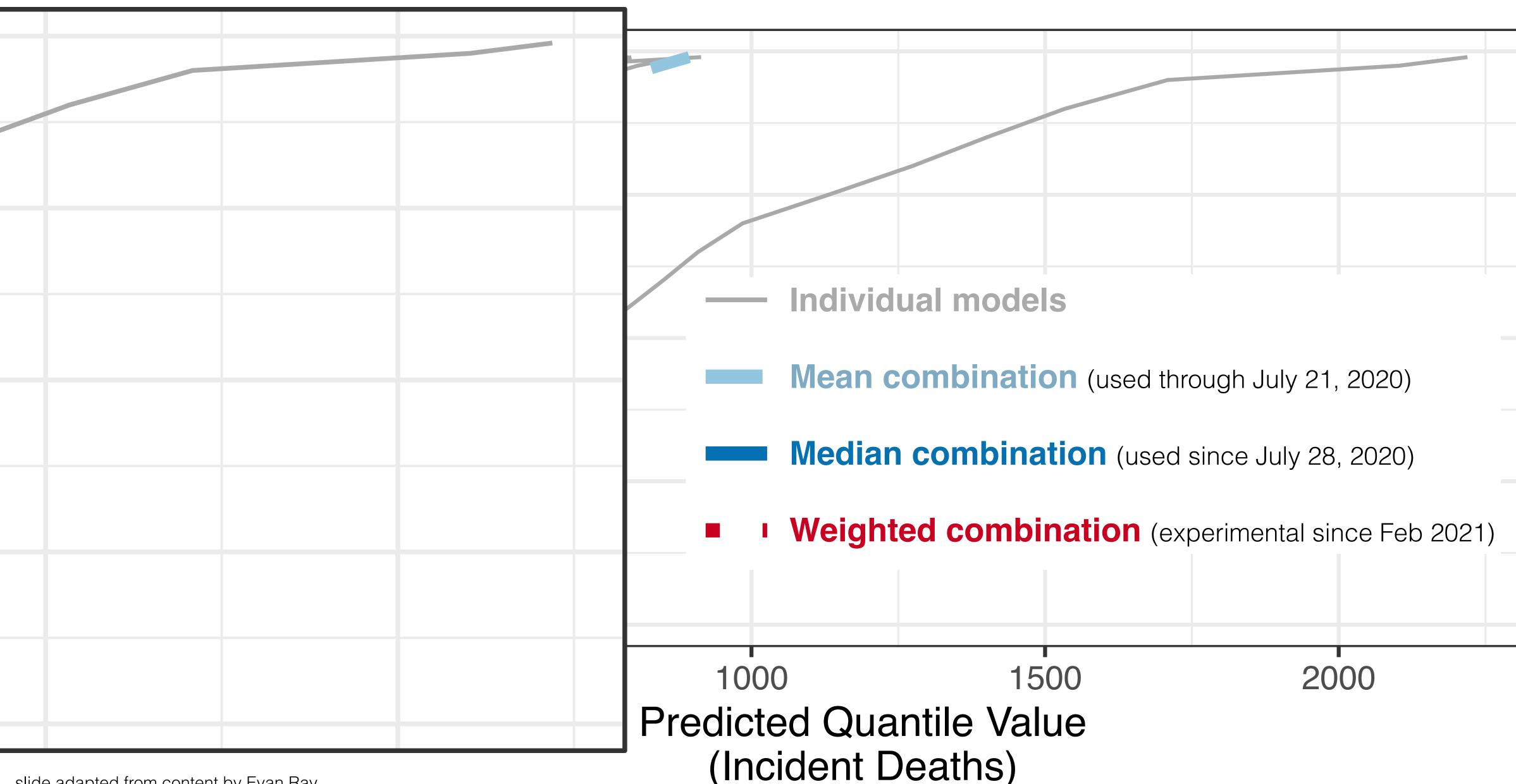




https://forecasters.org/blog/2021/09/28/on-the-predictability-of-covid-19/



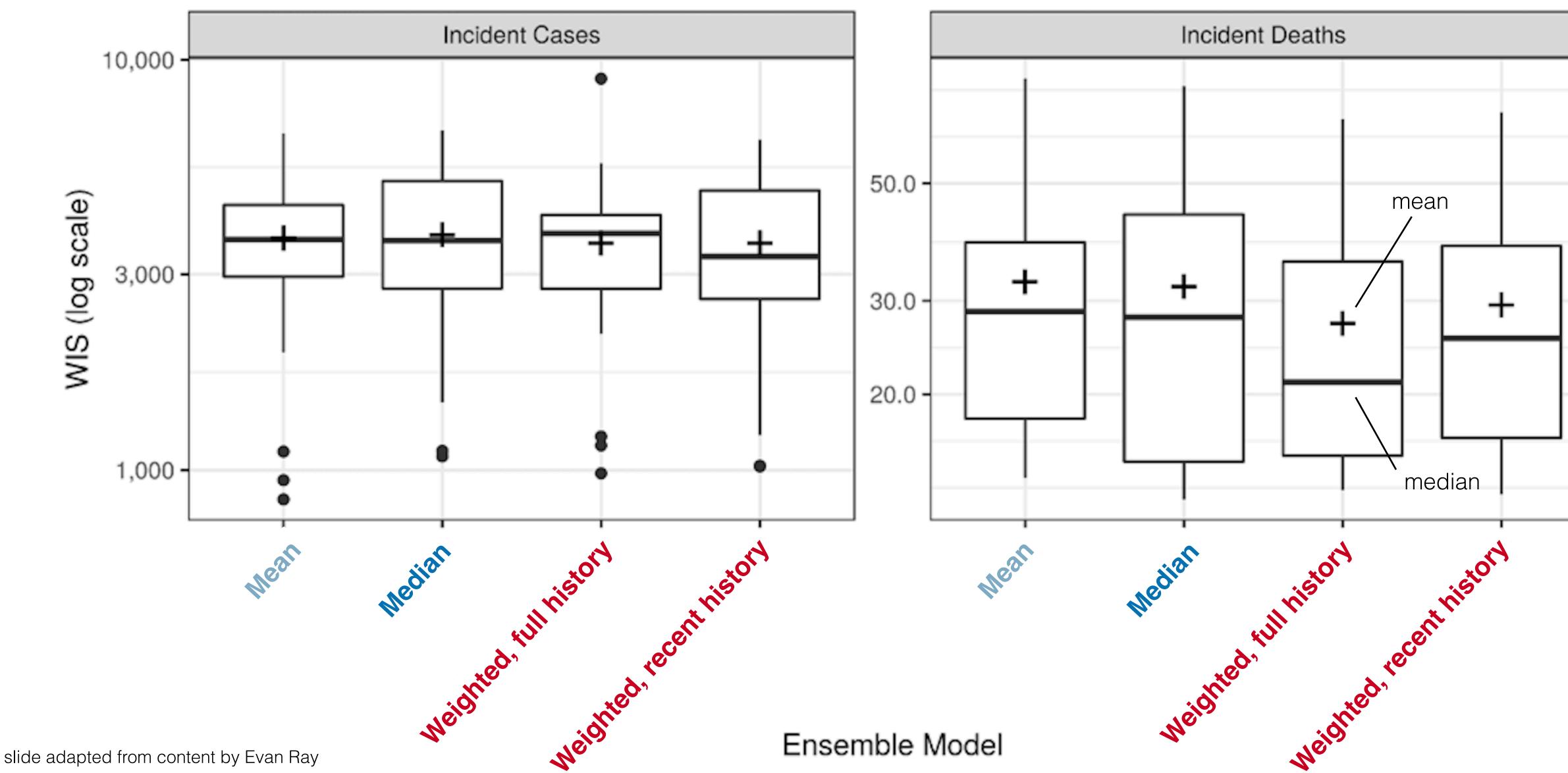
Building an Ensemble: View 2



slide adapted from content by Evan Ray



Weighted ensembles yield modest accuracy gains

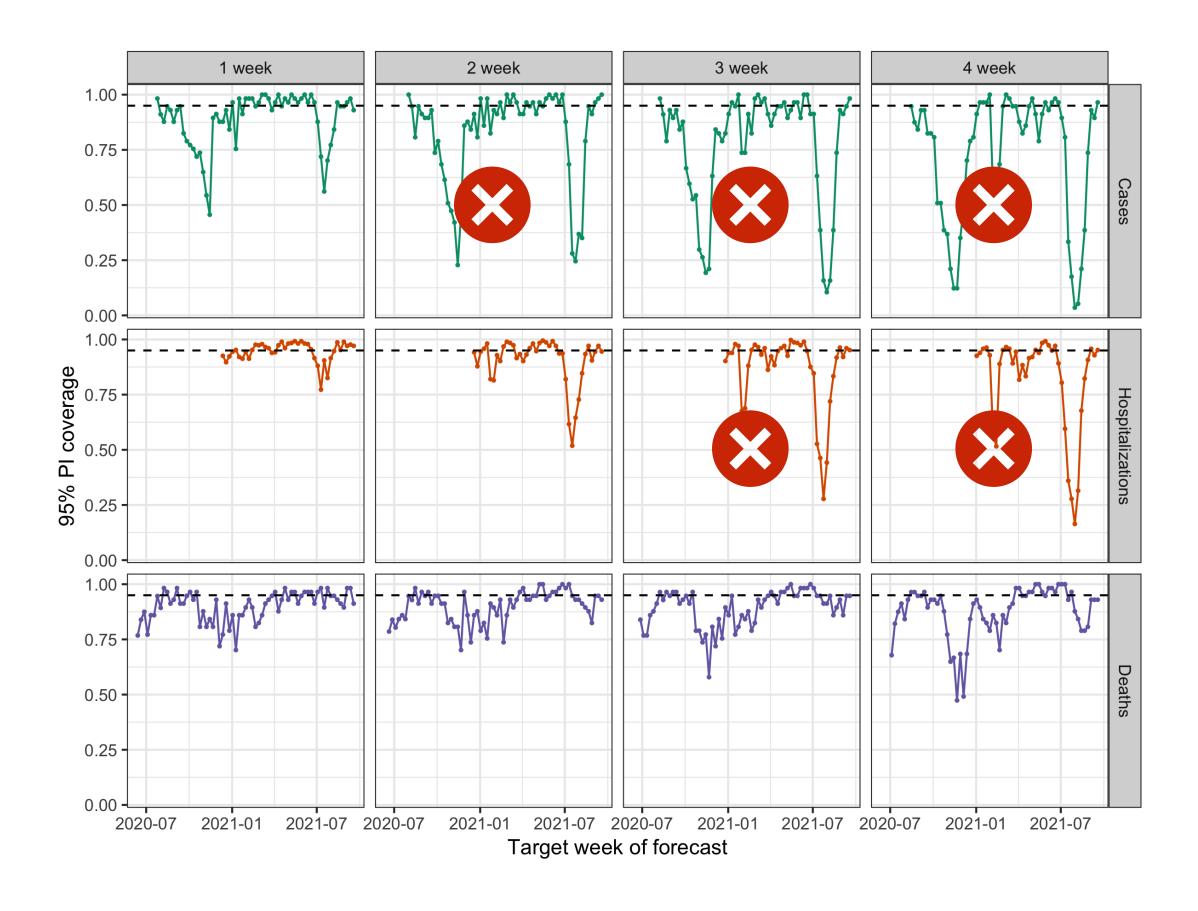






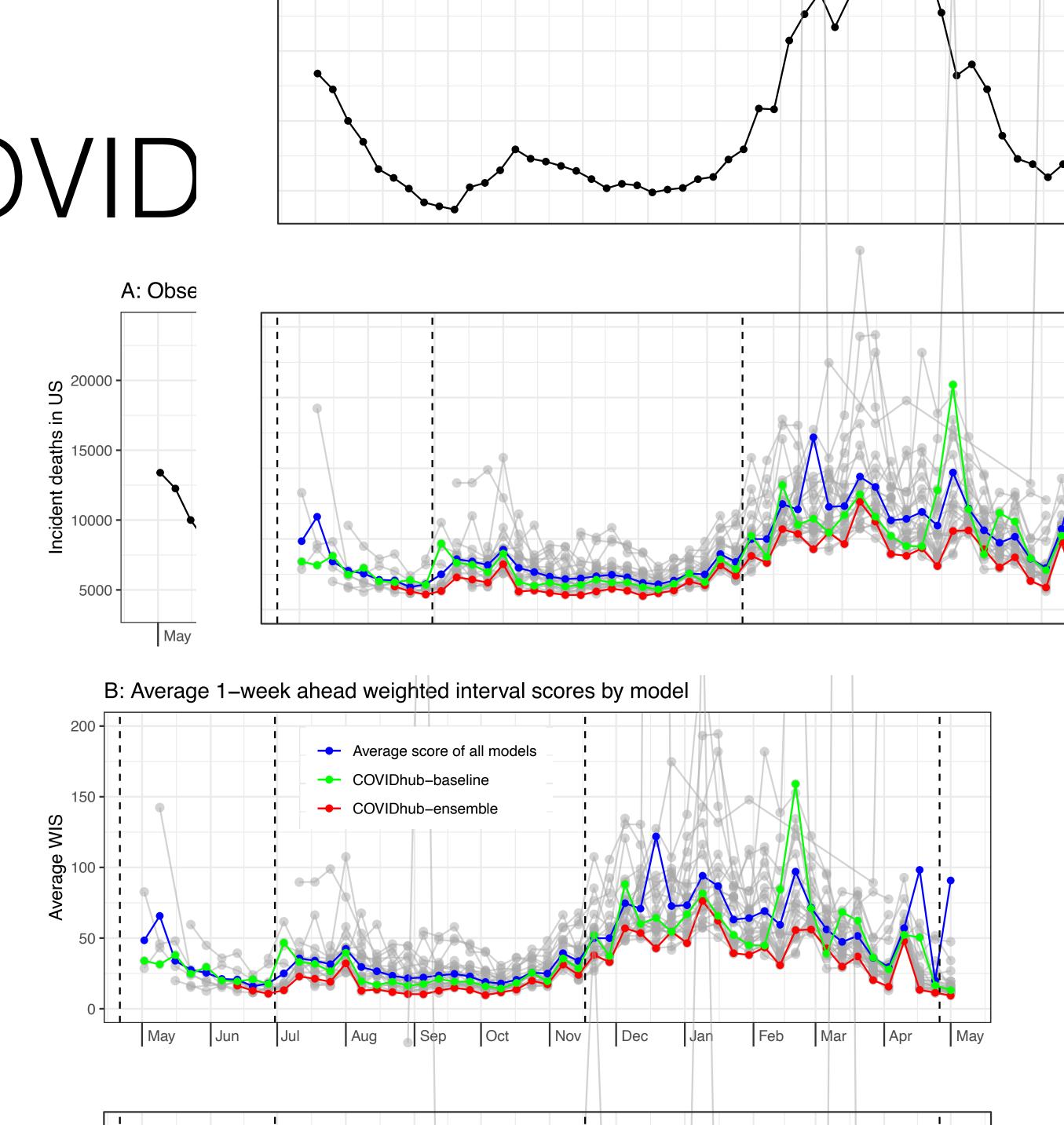
Lessons from COVID-19 forecasting

- 1. In the very near term, forecasts for all outcomes are usually accurate. For deaths, forecasts up to 4 weeks are reliable.
- 2. Treat any specific 4+ week-ahead prediction with skepticism! (Especially for cases.)



Lessons from COVID

- 3. Individual model performance varies substantially.
- 4. Data quality issues (e.g. revisions after the fact and imperfect "ground truth" measurements) pose challenges for models.



Lessons from COVID-19 forecasting

 Don't rely on one model, unless it is an ensemble.
 And even then, remain skeptical!

model	rel. WIS	95% cov.
COVIDhub-ensemble	0.54	0.94
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September 17, 2021

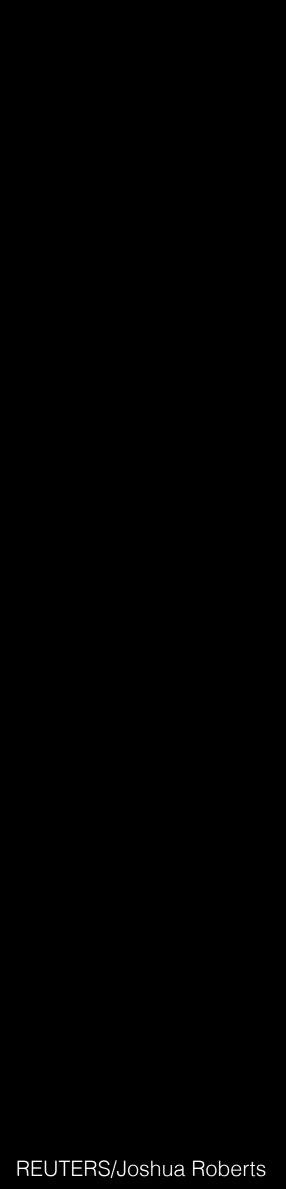
Remember.

water min throw wind.

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The use of multiple perspectives to gain insight into the truth is not just a statistical idea, but one rooted in story-telling.

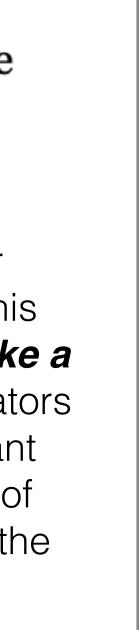


American Journal of Sociology > Volume 124, Number 2

Faulkner's Assembly of Memories into History: Narrative Networks in Multiple Times¹

John F. Padgett

The core stylistic problematic, indeed the obsession, for Faulkner was how **the diverse multiple perspectives** of his narrators and characters do or do not blend together to **make a collective ensemble**, which at minimum is gripping to narrators and which at maximum is true—in the sense that an elegant multiperspectival account emerges from the composition of partial perspectives, consistent with all known facts about the behaviors of characters in the story.



The use of multiple perspectives to gain insight into the truth is not just a statistical idea, but one rooted in story-telling.



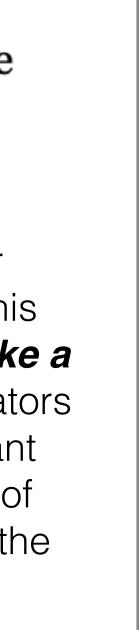
I'm telling you stories. Trust me. from "The Passion" by Jeanette Winterson

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The core stylistic problematic, indeed the obsession, for Faulkner was how *the diverse multiple perspectives* of his narrators and characters do or do not blend together to *make a collective ensemble*, which at minimum is gripping to narrators and which at maximum is true—in the sense that an elegant multiperspectival account emerges from the composition of partial perspectives, consistent with all known facts about the behaviors of characters in the story.





Team: Martha Zorn, Nutcha Wattanachit, Serena Wang, Ariane Stark, Li Shandross, Apurv Shah, Nicholas Reich, Evan Ray, Jarad Niemi, Vrushti Mody, Khoa Le, Abdul Kanji, Dasuni Jayawardena, Yuxin Huang, Katie House, Aaron Gerding, Estee Cramer, Matt Cornell, Alvaro J. Castro Rivadeneira, Andrea Brennen, Johannes Bracher

> **US CDC Collaborators**: Matthew Biggerstaff, Michael Johansson, Velma Lopez, Rachel Slayton, Jo Walker, and others

CMU Delphi Group: Ryan Tibshirani, Roni Rosenfeld, Logan Brooks, and others

Ensemble "advisors": Jacob Bien, Logan Brooks, Sebastian Funk, Tilmann Gneiting, Anja Muhlemann, Aaron Rumack, Ryan Tibshirani, and others

Modeling groups: Over 80 groups at various institutions have contributed forecasts







UMassAmherst

School of Public Health & Health Sciences

Biostatistics and Epidemiology

Thank you!

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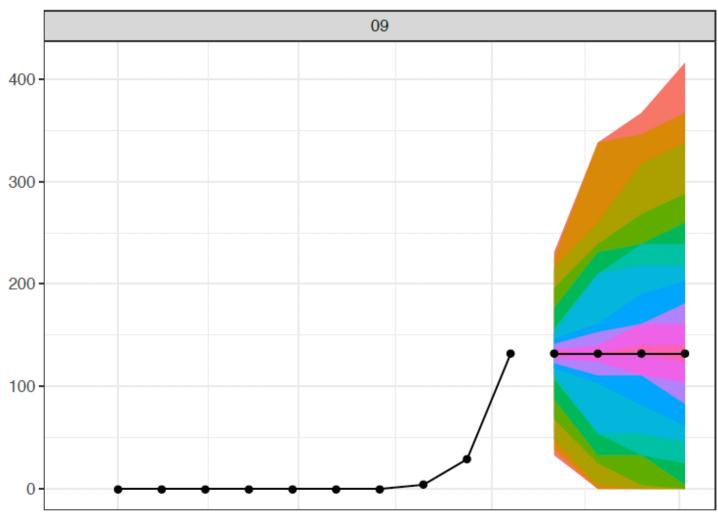
Evan Ray





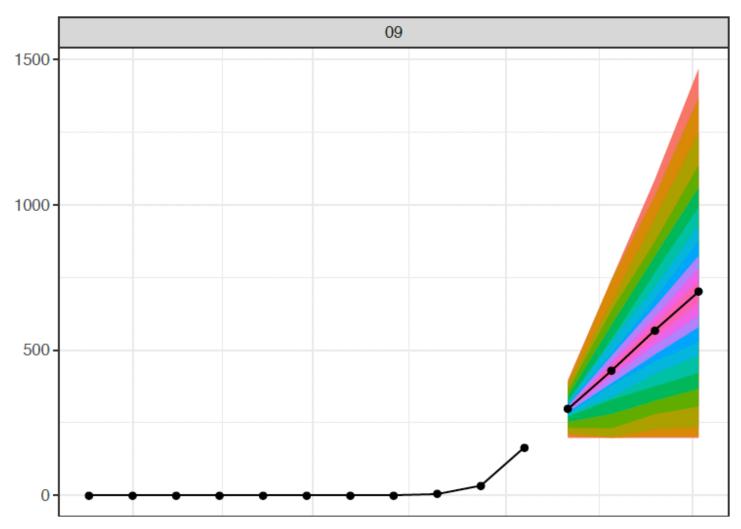
Baseline Model

- Different from flu forecasting baseline model! Not "seasonally" driven.
- Goal: Median predicted incidence is most recent observed incidence.



Incident Deaths

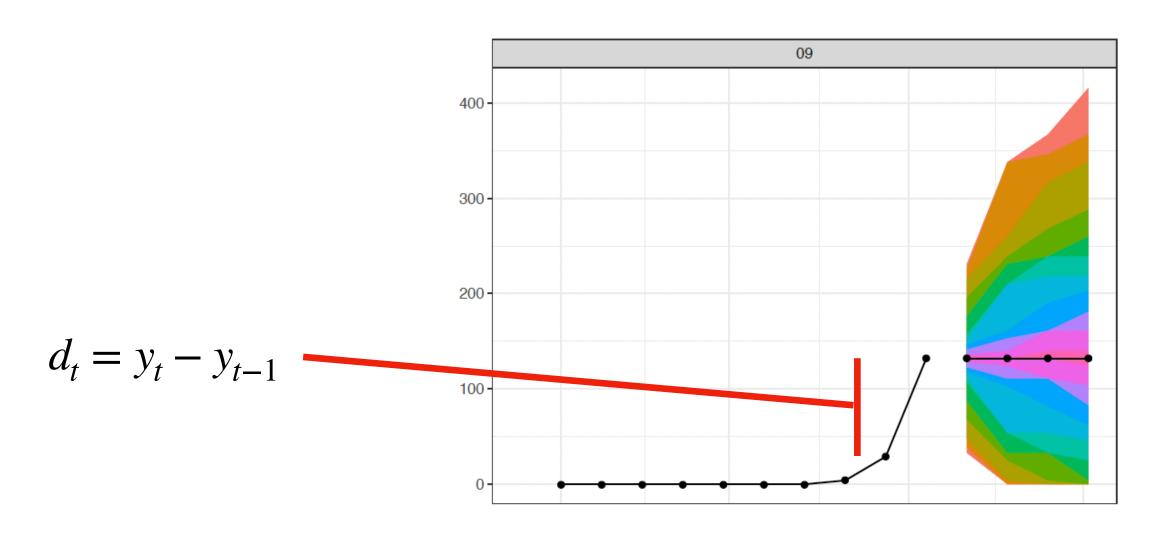
• Acknowledgment: idea adapted from a suggestion by Ryan Tibshirani (CMU). • Predictions of cumulative deaths derived from predictions of incident deaths.



Cumulative Deaths

Baseline Model

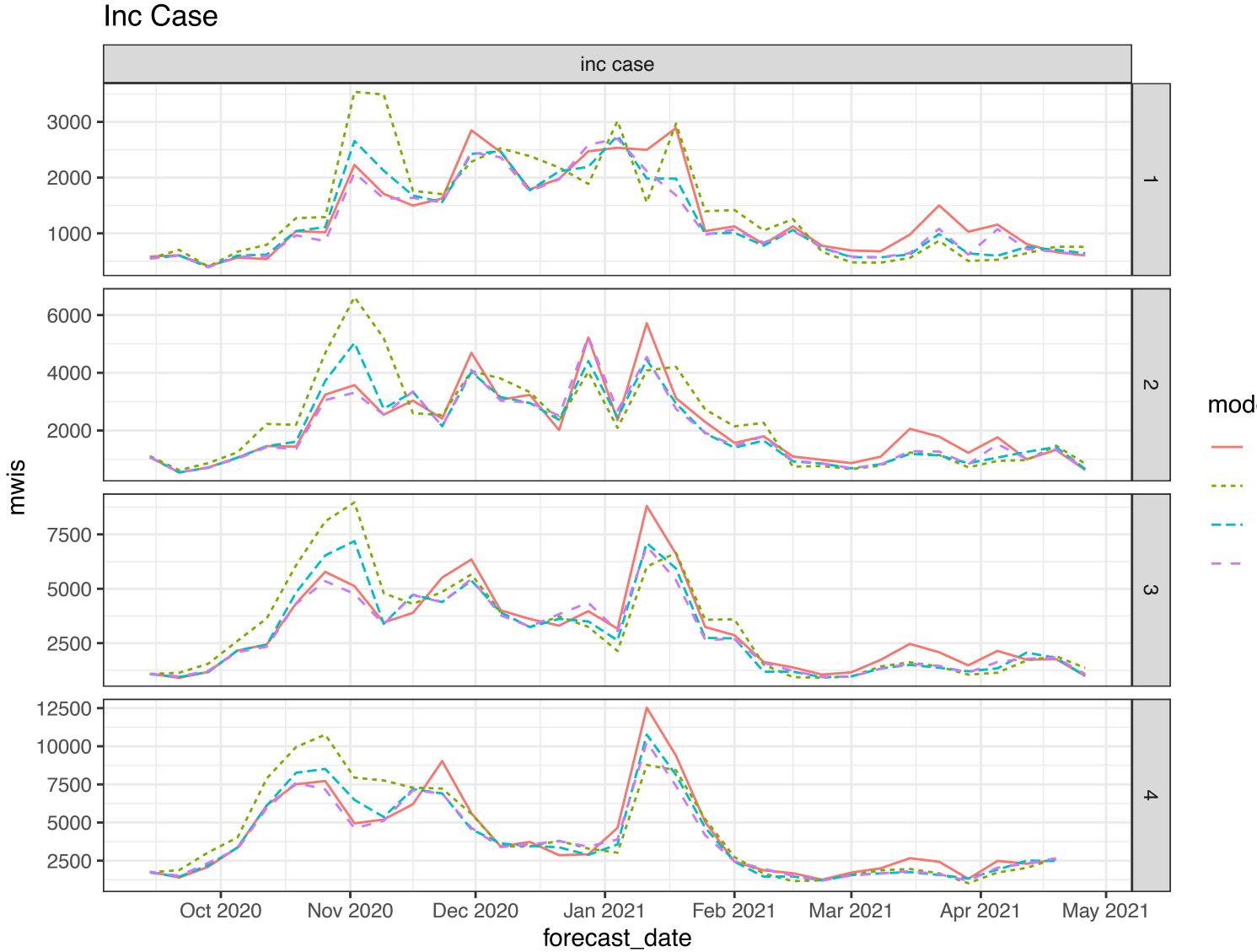
- Procedure:
 - Compute first differences of historical incidence:



- Collect first differences and mean means the second s
- the resulting distribution
- Iterate for horizons > 1
- Adjustments for "niceness":
 - Force median = last observed incidence
 - Truncate at 0

• Sample first differences and add to last observed incidence; take quantiles of

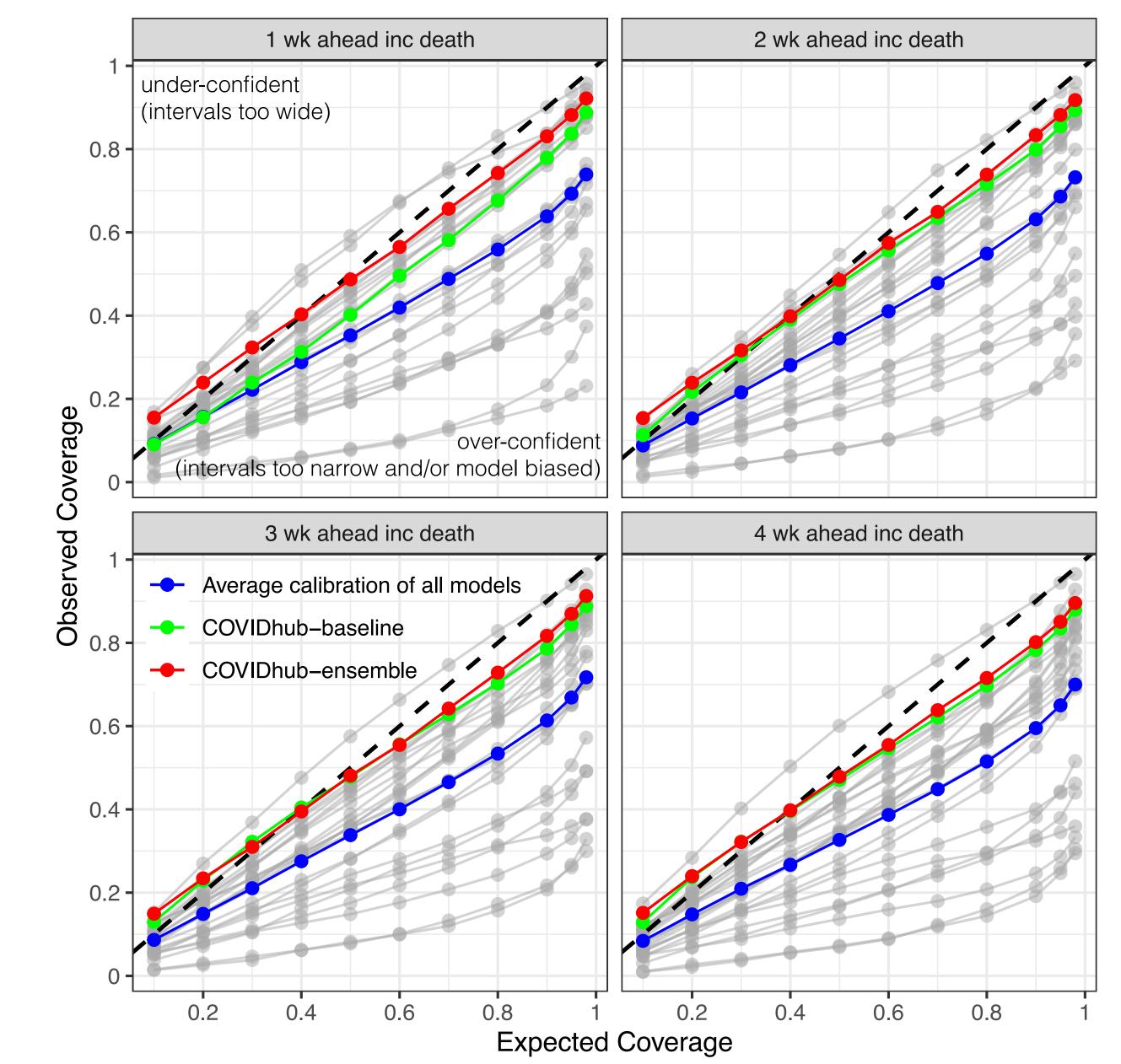
Evaluation Over Time – Cases

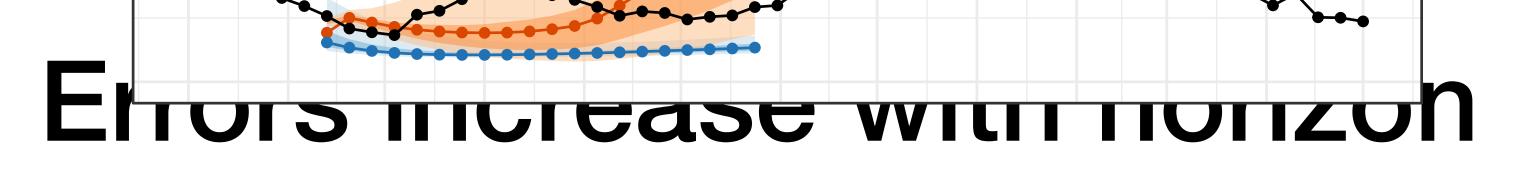


model_brief

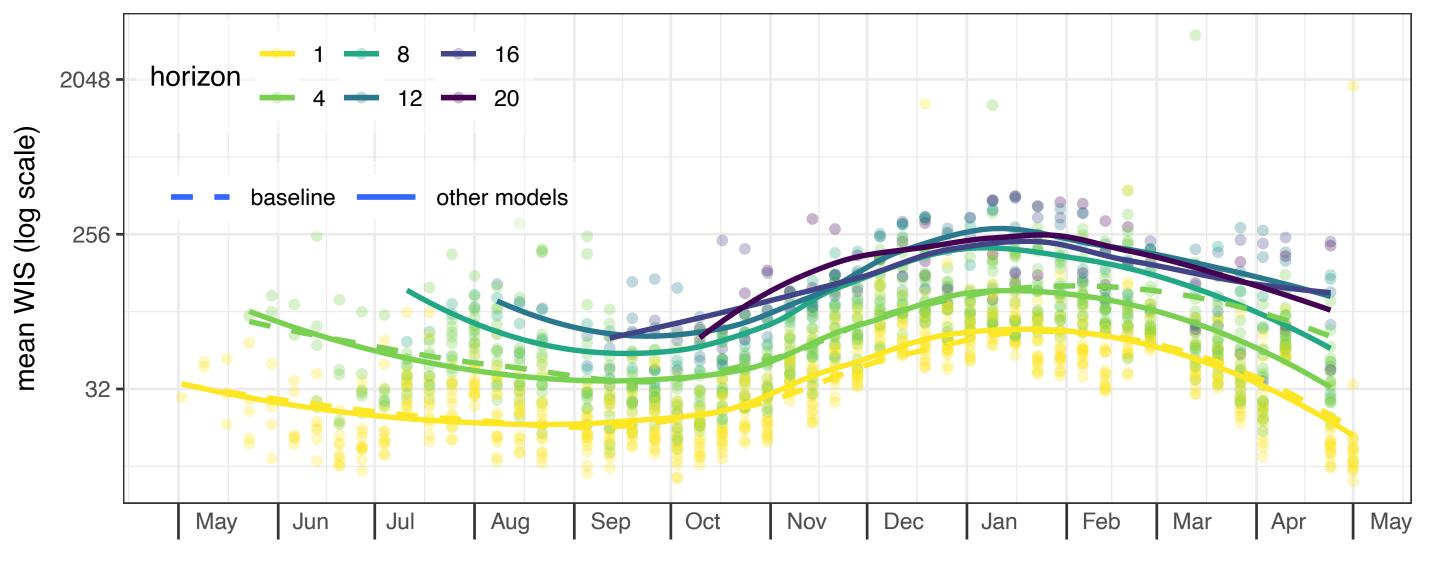
- convex_median=12-top_5
- ---- median-0-all
- --· median-12-top_5
- - rel_wis_weighted_median-12-top_5

Model calibration – Deaths

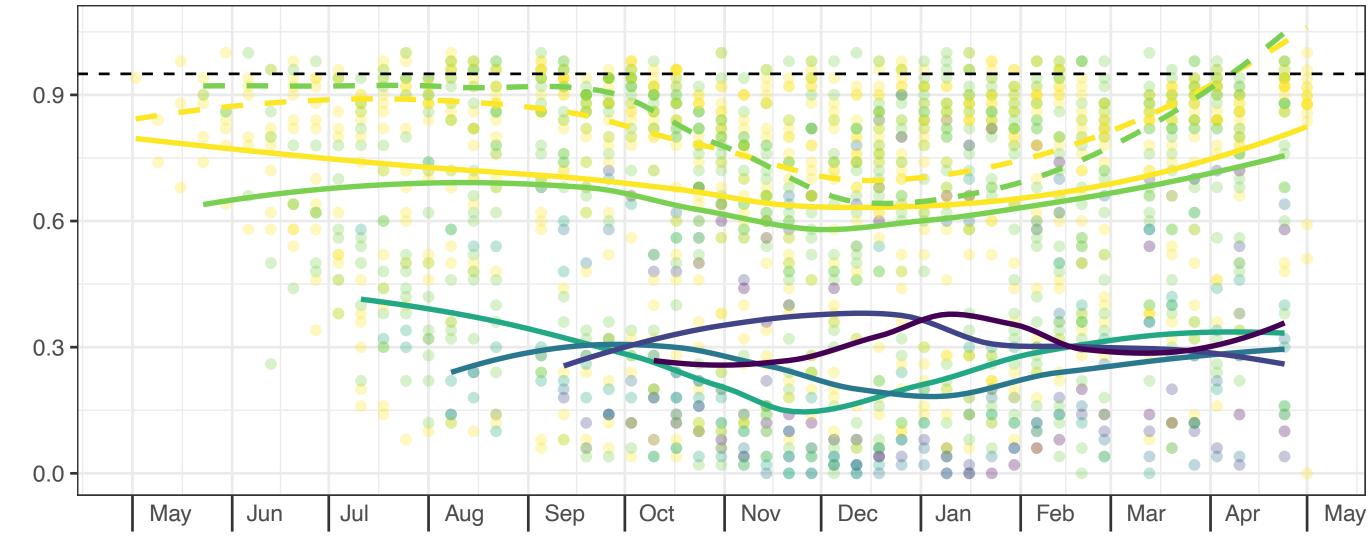




B: mean WIS across time, stratified by forecast horizon







95% Prediction Interval Coverage

C: 95% prediction interval coverage across time, stratified by forecast horizon